A first top partner hunter's guide

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Abstract: We provide a systematic effective lagrangian description of the phenomenology of the lightest top-partners in composite Higgs models. Our construction is based on symmetry, on selection rules and on plausible dynamical assumptions. The structure of the resulting simplified models depends on the quantum numbers of the lightest top partner and of the operators involved in the generation of the top Yukawa. In all cases the phenomenology is conveniently described by a small number of parameters, and the results of experimental searches are readily interpreted as a test of naturalness. We recast presently available experimental bounds on heavy fermions into bounds on top partners: LHC has already stepped well inside the natural region of parameter space.

Contents

1 Introduction

The exploration of the weak scale at the Large Hadron Collider is set to unveil the dynamics of electroweak symmetry breaking. A giant step in that direction was achieved this year with the discovery of a bosonic resonance, whose features are remarkably compatible with those of the Standard Model Higgs boson. Whether we like it or not, the main question now facing us concerns the role of naturalness in the dynamics of the newly discovered boson. Theoretically we can think of two broad scenarios that concretely realize naturalness: supersymmetry and compositeness. In the case of supersymmetry, the implications and the search strategies have been worked out in much greater detail than in

the case of compositeness. That is explained partly by the undisputable theoretical appeal of supersymmetry (gauge coupling unification, connection with string theory, etc.) and partly by the comfort of dealing with a perturbative set up. The difficulty in dealing with strong dynamics has instead, and for a long time, slowed down progress in the exploration of compositeness, and, in particular, progress on its objective phenomenological difficulties (mostly flavor, but also precision tests). Interesting ideas were indeed put forward early on [1, 2], but the absence of a weakly coupled approach prevented more concrete scenarios to appear. However, in the last decade, thanks in particular to the holographic perspective on compositeness, *semi-perturbative* scenarios have been depicted and studied [3].[1] Even though a very compelling single model did not cross our horizon, we believe we have learned how to broadly depict interesting scenarios, while remaining sufficiently agnostic on the details (see for instance [4]). The first aspect of an interesting set up is that the Higgs is a pseudo-NG-boson associated with the spontaneous breakdown of an approximate global symmetry. The second aspect is that flavor arises from *partial compositeness*: the quarks and leptons acquire a mass by mixing with composite fermions. Partial compositeness, although much more convincing than the alternatives, does not, by itself, lead to a fully realistic flavor scenario. This is because of constraints from ϵ_K [5], electric dipole moments and lepton flavor violation (see ref. [6] for a recent appraisal). In a realistic scenario partial compositeness should likely be supplemented by additional symmetries. In any case, and regardless of details, a robust feature is that the Higgs potential is largely determined by the dynamics associated with the top quark and the composite states it mixes to, the so-called top partners. That is in a sense obvious and expected, as the top quark, because of its large coupling, color multiplicity and numerics already contributes the leading quadratically divergent correction to the Higgs mass within the SM. It is nonetheless useful to have depicted a scenario that concretely realizes that expectation. The naturalness of electroweak symmetry breaking depends then on the mass of the fermionic top-partners. That is in close analogy with the supersymmetric case, where naturalness is largely controlled by the mass of the bosonic top partners, the stops.

The case of light stops in supersymmetry is being actively considered both theoretically and experimentally. One main goal is to effectively cover all regions of parameter space, without being swamped by the less relevant parameters. Simplified models or motivated assumptions like "natural susy" [7–9] offer a convenient way to achieve that goal. In the reduced parameter space (featuring stop mass parameters and possibly the gluino or lightest neutralino mass), the constraints from of experimental searches offer a direct and largely model independent appraisal of naturalness. The goal of this paper is to provide a similar simplified approach to describe the results of experimental searches for top partners. We will focus on the composite Higgs scenario based on the minimal coset SO(5)/SO(4). The basic simplifying assumption is that the spectrum has the structure depicted in figure 1, where one SO(4) multiplet of colored Dirac fermions Ψ is parametrically lighter than the other states. As already illustrated in ref. [10] for the case of bosonic resonances,

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[1]By *semi-perturbative* here we mean that in these models, typified by warped compactifications, there exists a sufficiently interesting subset of questions, even involving physics at energies well above the weak scale, that can be addressed using perturbation theory.
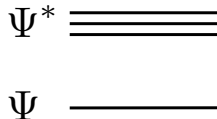
Figure 1. Schematic picture of the spectrum.

in that limit one expects the dynamics of Ψ to be described by a weakly coupled effective lagrangian. Therefore the simplified model, at leading order in an expansion in loops and derivatives, can be consistently described by a finite number of parameters. Moreover symmetry and selection rules, via the Callan-Coleman-Wess-Zumino (CCWZ) [11] construction, reduce the number of relevant parameters. It is obviously understood that the limiting situation presented by the simplified model is not expected to be precisely realized in a realistic scenario. However, a realistic situation where the splitting with the next-to-lightest multiplet is of the order M_Ψ is qualitatively already well described by the simplified model. Only if the splitting were parametrically smaller than M_Ψ would there be dramatic changes. We should also stress that our models are truly minimal, in that they do not even possess sufficient structure (states and couplings) to make the Higgs potential calculable. In principle we could add that structure. For instance by uplifting our multiplet Ψ to a full split SO(5) multiplet, like in a two site model, we could make the Higgs potential only logarithmically divergent, thus controlling its size in leading log approximation, and making the rough connection between M_Ψ and naturalness more explicit along the lines of [12] (see also [13–15] for a similar construction). We could even go as far as making the one loop Higgs potential finite with a three site model [16, 17], or by imposing phenomenological Weinberg sum-rules [18, 19]. However in these less minimal models the first signals at the LHC would still be dominated by the lightest SO(4) multiplet, whatever it may be. The point is that while the contribution of the heavier multiplets does not decouple when focussing on a UV sensitive quantity like the Higgs potential, it does decouple when considering the near threshold production of the lightest states. For the purpose of presenting the results of the LHC searches in an eloquent way, the simplified model is clearly the way to go. There already exists a literature on simplified top partner models in generic composite Higgs scenarios [20–22], where the role of symmetry is not fully exploited. Focussing on the minimal composite Higgs model based on SO(5)/SO(4), our paper aims at developing a systematic approach where all possible top partner models are constructed purely on the basis of symmetry and selection rules.

In the end we shall derive exclusion plots in a reduced parameter space, which in general involves the mass and couplings of the top-partner Ψ. Now, even though these are not the parameters of a fundamental model, given their overall size, we can roughly estimate how natural the Higgs sector is expected to be. We can then read the results of searches as a test of the notion of naturalness. To make that connection, even if qualitative, we must specifiy the dynamics that gives rise to the top Yukawa. As discussed in [23], there are several options, each leading to a different structure of the Higgs potential and thus to a different level of tuning. The common feature of all scenarios is that the top partners need

to be light for a reasonably natural theory, the way the tuning scales with the top-partners' mass is instead different in each case. In this paper we focus on the possibility that the right handed top quark t_R is a SO(4) singlet belonging to the strong sector, therefore the top Yukawa simply arises from an SO(5) breaking perturbation of the form

$$\lambda_L q_L \mathcal{O}_R + \text{h.c.}.\tag{1.1}$$

Here $\mathcal{O}_R$ is a composite operator, which in the low energy theory maps to Ht_R, thus giving rise to a top Yukawa coupling $y_t \sim \lambda_L$. The operator O_R however also interpolates in general for massive states, the top partners. Now, from simple power counting, and also from explicit constructions [16], at leading order in the breaking parameter λ_L we expect the Higgs potential to have the form

$$V(h) = \frac{3y_t^2 m_*^2}{16\pi^2}\left\{ah^2 + \frac{b}{2}\frac{h^4}{f^2} + \frac{c}{3!}\frac{h^6}{f^4} + \dots\right\}.\tag{1.2}$$

where $a, b, c, \dots$ are coefficients expected to be $O(1)$, f is the decay constant of the σ-model, while m_* broadly indicates the mass scale of the top partners. Then, since Ψ is, ideally, the lightest top-partner we have $M_\Psi \lesssim m_*$. Given m_* and f, the measured values $v \equiv \langle h \rangle = 246\,\text{GeV}$ and $m_h = 125\,\text{GeV}$, may require a tuning of a and b below their expected $O(1)$ size. More explicitly one finds

$$a = \frac{m_h^2}{m_*^2}\frac{4\pi^2}{3y_t^2} \simeq \left(\frac{430\,\text{GeV}}{m_*}\right)^2\tag{1.3}$$

and, defining the top-partner coupling as $g_* \equiv m_*/f$ according to ref. [4],

$$b = \frac{m_h^2}{m_t^2}\frac{2\pi^2}{3g_*^2} \simeq \frac{4}{g_*^2}.\tag{1.4}$$

By these equations we deduce that in the most natural scenario the top partners should not only be light (say below a TeV) but also not too strongly coupled. While of course the whole discussion is very qualitative, we still believe eqs. (1.3)–(1.4) give a valid rule of thumb for where the top partners should best be found. It is with eqs. (1.3)–(1.4) in mind that one should interpret the results of the searches for top partners. Notice that while naturalness favors sub-TeV fermionic resonances, electroweak precision constraints favor instead bosonic resonances above 2–3 TeV. A technically natural and viable model should therefore be more complex than a generic composite model described by a single scale. This situation closely resembles that of supersymmetric models, where the light squark families and the gluinos are pushed up by direct searches, while technical naturalness demands the stops to be as light as possible.

This paper is organized as follows. In section 2 we discuss the structure of the models and their main features such as the mass spectrum and the couplings of the top partners. Then, in section 3 we turn to analyse the phenomenology of the top partners, their production mechanisms and decay channels, highlighting the most relevant channels to focus

LHC searches on. The bounds on the model parameters are derived in section 4, using the LHC data available at present.[2] Finally, our concluding remarks are collected in section 5.

2 The models

Our first goal is to develop a simplified description of the top partners, suited for studying the phenomenology of their production at the LHC. These simplified models should capture the robust features of more complete explicit constructions[3] or, better, of a putative general class of underlying theories. In particular, robust, and crucial, features are the pNGB nature of the Higgs and the selection rules associated with the small breaking of the corresponding global symmetry. We will see below that these features strongly constraints the structure of the spectrum and of the couplings of the top partners, similarly to what was found in ref. [16] for the case of partial t_R compositeness.

We thus assume that the Higgs is the pNGB of the minimal coset SO(5)/SO(4) and construct Lagrangians that respect the non-linearly realized SO(5) invariance. We follow the standard CCWZ construction [11], whose detailed formulation for our coset is described in appendix A. The CCWZ methodology has been first employed to model the top partners in ref. [18]. The central objects are the Goldstone boson 5×5 matrix U and the d_μ and e_μ symbols constructed out of U and its derivative. The top partner field Ψ has definite transformation properties under the unbroken SO(4) group. We will consider two cases, Ψ transforming in the $r_\Psi = \mathbf{4}$ or $r_\Psi = \mathbf{1}$ of SO(4).

In our construction the right-handed top quark t_R emerges as a chiral bound state of the strong dynamics. t_R must thus belong to a complete multiplet of the unbroken subgroup SO(4), and, given we do not want extra massless states, it must be a singlet. That does not yet fully specify its quantum numbers. This is because, in order to reproduce the correct hypercharge, one must enlarge the global symmetry by including an extra unbroken U(1)$_X$ factor and define the hypercharge as $Y = T_R^3 + X$, where T_R^3 is the third SU(2)$_R$ generator of SO(5).[4] Therefore the coset is actually SO(5) $\times$ U(1)$_X$/SO(4) $\times$ U(1)$_X$, t_R has X charge equal to 2/3 while the Higgs is X neutral (its hypercharge coincides with its T_R^3 charge).

A second assumption concerns the coupling of the elementary fields, i.e. the SM gauge fields W_μ and B_μ and the elementary left-handed doublet $q_L = (t_L, b_L)$, to the strong sector.[5] The EW bosons are coupled by gauging the SM subgroup of SO(5) $\times$ U(1)$_X$. The q_L is assumed to be coupled *linearly* to the strong sector, following the hypothesis of partial

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[2]While this work was being completed ATLAS [24] and CMS [25] presented dedicated searches for top partners, which we did not include in our analysis. From a preliminary investigation we expect mild changes in our results from these new data because both the ATLAS and the CMS searches are optimized to detect pair production. As we will discuss in the conclusions, a radical improvement of the bounds could perhaps be achieved, with the present energy and luminosity, but only with searches dedicated to single production.

[3]See [23] for a complete calculable model with totally composite t_R, analogous holographic 5d models could be formulated following the approach of ref. [3].

[4]See appendix A for the explicit form of the generators.

[5]The light quark families and the leptons will not be considered here because their couplings are most likely very weak.

compositeness [2]. In the UV Lagrangian this coupling has therefore the form

$$\mathcal{L}_{\text{mix}}^{\text{UV}} = y\, \overline{q}_L^\alpha \Delta^*_{\alpha\, I_{\mathcal{O}}} \mathcal{O}^{I_{\mathcal{O}}} + \text{h.}c. \equiv y\, \left(\overline{Q}_L\right)_{I_{\mathcal{O}}} \mathcal{O}^{I_{\mathcal{O}}} + \text{h.}c.\,, \tag{2.1}$$

where $\mathcal{O}$ is an operator of the strong sector that transforms in some representation $r_{\mathcal{O}}$ of $\text{SO}(5) \times \text{U}(1)_X$. The choice of $r_{\mathcal{O}}$ is, to some extent, free. Minimality, and the aim of reproducing explicit models considered in the literature, led us to consider two cases: $r_{\mathcal{O}} = \mathbf{5_{2/3}}$ and $\mathbf{r_{\mathcal{O}} = 14_{2/3}}$.[6] Notice that the $\text{U}(1)_X$ charge of the operators must be equal to the one of the t_R in order for the top mass to be generated after EWSB. In total, depending on whether the top partners will be in the $\mathbf{4_{2/3}}$ or in the $\mathbf{1_{2/3}}$ of the unbroken $\text{SO}(4)$, we will discuss four models named $\mathbf{M4_5}$, $\mathbf{M4_{14}}$ and $\mathbf{M1_5}$, $\mathbf{M1_{14}}$ respectively. The classification of the various models is summarized in table 1.

The explict breakdown of $\text{SO}(5)$ due to y in eq. (2.1) gives rise to a leading contribution to the Higgs potential $V(h)$. However, in order to be able to tune the Higgs vacuum expectation value v to be much smaller that its natural scale f, one may need to tune among themselves contributions to $V(h)$ with a different functional dependence on h/f. In the case of $\mathbf{r_{\mathcal{O}} = 14_{2/3}}$, the top Yukawa seed y itself gives rise to two independent structures, whose coefficients can be so tuned that $v/f \ll 1$. On the other hand, in the case of $\mathbf{r_{\mathcal{O}} = 5_{2/3}}$, the leading contribution to the potential consist of just one structure $\propto \sin^2 h/f \cos^2 h/f$, with well defined, non-tunable, minima and maxima. In the latter case then, in order to achieve $v \ll f$, one should assume there exists an additional of $\text{SO}(5)$ breaking coupling whose contribution to the potential competes with that of the top. If this additional coupling does not involve the SM fields, which seems resonable, then its contribution to V will arise at tree level. In order not to outcompete the top contribution, which arises at loop level, then this coupling should be so suppressed that its relative impact on strong sector quantities is of order $O(y^2/16\pi^2)$. The latter should be compared to the effects of relative size $(y/g_\Psi)^2$ induced at tree level by the mixing in eq. (2.1) and accounted for in this paper. We conclude that, even when an extra $\text{SO}(5)$ breaking coupling is needed, it is not likely to affect the phenomenology of top partners in a quantitatively significant way.

Now back to the top partners. Our choices of their quantum numbers correspond to those obtained in explicit constructions. However our choice could also be motivated on general grounds by noticing the operators $\mathcal{O}$ interpolate for particles with the corresponding quantum numbers. By decomposing $\mathcal{O}$ under the unbroken $\text{SO}(4)$ we obtain, respectively, $\mathbf{5_{2/3} = 4_{2/3} + 1_{2/3}}$ and $\mathbf{14_{2/3} = 4_{2/3} + 1_{2/3} + 9_{2/3}}$. In both cases we expect to find a $\mathbf{4_{2/3}}$ and/or a $\mathbf{1_{2/3}}$ in the low-energy spectrum. It could be also interesting to study top partners in the $\mathbf{9_{2/3}}$, but this goes beyond the scope of the present paper.

The coupling of eq. (2.1) breaks the $\text{SO}(5) \times \text{U}(1)_X$ symmetry explicitly, but it must of course respect the SM group. This fixes unambiguously the form of the tensor Δ and thus of the *embeddings*, $(Q_L)_{I_{\mathcal{O}}} = \Delta_{\alpha\, I_{\mathcal{O}}} q_L^\alpha$, of the elementary q_L in $\text{SO}(5) \times \text{U}(1)_X$ multiplets.

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[6]Another possible option considered in the literature is $r_{\mathcal{O}} = \mathbf{4_{1/6}}$. However this option is not available once t_R is chosen to be a $\text{SO}(4)$ singlet: the top would not acquire a mass. It should also be remarked that, regardless of the nature of t_R, $r_{\mathcal{O}} = \mathbf{4_{1/6}}$ is disfavored when considering dangerous tree level corrections to the $Zb\bar{b}$ vertex [26, 27].

	$r_{\mathcal{O}} = \mathbf{5_{2/3}}$	$r_{\mathcal{O}} = \mathbf{14_{2/3}}$
$r_{\Psi} = \mathbf{4_{2/3}}$	$\mathbf{M4_5}$	$\mathbf{M4_{14}}$
$r_{\Psi} = \mathbf{1_{2/3}}$	$\mathbf{M1_5}$	$\mathbf{M1_{14}}$

Table 1. The nomenclature of the four models considered in the present paper, defined by the choices of the representations $r_{\Psi}, r_{\mathcal{O}}$.

For the **5** and the **14**, respectively the fundamental and the two-indices symmetric traceless tensor, we have

$$
(Q_L^{\mathbf{5}})_I = \frac{1}{\sqrt{2}} \begin{pmatrix} ib_L \\ b_L \\ it_L \\ -t_L \\ 0 \end{pmatrix}, \qquad (Q_L^{\mathbf{14}})_{I,J} = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 & 0 & 0 & 0 & ib_L \\ 0 & 0 & 0 & 0 & b_L \\ 0 & 0 & 0 & 0 & it_L \\ 0 & 0 & 0 & 0 & -t_L \\ ib_L & b_L & it_L & -t_L & 0 \end{pmatrix}. \qquad (2.2)
$$

Though explicitly broken, the $\mathrm{SO}(5) \times \mathrm{U}(1)_X$ group still gives strong constraints on our theory. Indeed the elementary-composite interactions of eq. (2.1) formally respect the symmetry provided we formally assign suitable transformation properties to the embeddings. Under $g \in \mathrm{SO}(5)$ we have

$$
(Q_L^{\mathbf{5}})_I \rightarrow g_I^{I'} (Q_L^{\mathbf{5}})_{I'}, \qquad (Q_L^{\mathbf{14}})_{IJ} \rightarrow g_I^{I'} g_J^{J'} (Q_L^{\mathbf{14}})_{I'J'}, \qquad (2.3)
$$

while the $\mathrm{U}(1)_X$ charge is equal to 2/3 in both cases. We will have to take into account this symmetry in our constructions.

2.1 Effective Lagrangians

Based on the symmetry principles specified above we aim at building phenomenological effective Lagrangians for the q_L, the composite t_R and the lightest top partner states Ψ. The basic idea is that our Lagrangians emerge from a "complete" theory by integrating out the heavier resonances in the strong sector. We thus need to rely on some qualitative description of the dynamics in order to estimate the importance of the various effective operators. We follow the "SILH" approach of ref. [4] and characterize the heavy resonances in terms of a single mass scale m_* and of a single coupling $g_* = m_*/f$. As we already suggested in the introduction, parametrizing the strong sector in terms of a single scale is probably insufficient: a $125\,\mathrm{GeV}$ Higgs suggests that the mass scale of the fermionic resonances should be slightly lower than that of the vectors. For our purposes the relevant scale m_* should then be identified with the mass scale of the fermionic sector. We thus adopt the following power-counting rule

$$
\mathcal{L} = \sum \frac{m_*^4}{g_*^2} \left(\frac{y\, q_L}{m_*^{3/2}} \right)^{n_{\mathrm{el}}} \left(\frac{g_* \Psi}{m_*^{3/2}} \right)^{n_{\mathrm{co}}} \left(\frac{\partial}{m_*} \right)^{n_{\partial}} \left(\frac{\Pi}{f} \right)^{n_{\pi}}, \qquad (2.4)
$$

where $\Pi = \Pi^{1,\dots,4}$ denotes the canonically normalized four real Higgs field components and f is the Goldstone decay constant. Notice the presence of the coupling y that accompanies

(due to eq. (2.1)) each insertion of the elementary q_L. Analogously the operators involving the SM gauge fields, omitted for shortness from eq. (2.4), should be weighted by g_{SM}/m_*. The t_R is completely composite and therefore it obeys the same power-counting rule as the top partner field Ψ.

Two terms in our effective Lagrangian will *violate* the power-counting. One is the kinetic term of the elementary fields, which we take to be canonical, while eq. (2.4) would assign it a smaller coefficient, $(y/g_*)^2$ in the case of fermions and $(g/g_*)^2$ in the case of gauge fields. This is because the elementary field kinetic term does not emerge from the strong sector, it was already present in the UV Lagrangian with $\mathcal{O}(1)$ coefficient. Indeed it is precisely because their kinetic coefficient is bigger than what established in eq. (2.4), that the elementary fields have a coupling weaker than g_*. The other term violating power-counting is the *mass* of the top partners, which we denote by M_Ψ. We assume $M_\Psi < m_*$ in order to justify the construction of an effective theory in which only the top partners are retained while the other resonances are integrated out. The ratio M_Ψ/m_* is our expansion parameter. We will therefore obtain accurate results only in the presence of a large separation, $M_\Psi \ll m_*$, among the lightest state and the other resonances.[7] However already for a moderate separation, $M_\Psi \lesssim m_*$, or even extrapolating towards $M_\Psi \simeq m_*$, our models should provide a valid qualitative description of the relevant physics. Nevertheless for a more careful study of the case of small separation our setup should be generalized by incorporating more resonances in the effective theory.

2.1.1 Top partners in the fourplet

First we consider models $\mathbf{M4}_5$ and $\mathbf{M4}_{14}$, in which the top partners are in the $\mathbf{4}_{2/3}$. In this case the top partner field is

$$\Psi = \frac{1}{\sqrt{2}} \begin{pmatrix} iB - iX_{5/3} \\ B + X_{5/3} \\ iT + iX_{2/3} \\ -T + X_{2/3} \end{pmatrix}, \tag{2.5}$$

and it transforms, following CCWZ, as

$$\Psi_i \to h(\Pi; g)_i^{\ j} \Psi_j, \tag{2.6}$$

under a generic element g of SO(5). The 4×4 matrix h is defined by eqs. (A.7) and (A.8) and provides a non-linear representation of the full SO(5). The four Ψ components decompose into two SM doublets (T, B) and $(X_{5/3}, X_{2/3})$ of hypercharge 1/6 and 7/6 respectively. The first doublet has therefore the same quantum numbers as the (t_L, b_L) doublet while the second one contains a state of exotic charge 5/3 plus another top-like quark $X_{2/3}$.

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[7]An organizing principle, termed *partial UV completion* (PUV), to consistently construct an effective lagrangian for a parametrically light resonance was proposed in ref. [10]. There the focus was on the more involved case of vector and scalar resonances. According to PUV, the couplings involving the lighter resonance should roughly saturate the strength g_* when extrapolated at the scale m_*. We refer to ref. [10] for a more detailed discussion. The effective lagrangians we construct in this paper automatically satisfy PUV in the range of parameters suggested by the power counting rule in eq. (2.4).

When the q_L is embedded in the $\mathbf{5_{2/3}}$, i.e. in model $\mathbf{M4}_5$, the leading order Lagrangian is

$$\mathcal{L}^{\mathbf{M4}_5} = i\,\bar{q}_L \slashed{D}\, q_L + i\,\bar{t}_R \slashed{D}\, t_R + i\,\bar{\Psi}(\slashed{D} + i\slashed{e})\Psi - M_\Psi \bar{\Psi}\Psi$$
$$+ \left[i\,c_1 \left(\bar{\Psi}_R\right)_i \gamma^\mu d_\mu^i\, t_R + yf\,(\overline{Q}_L^{\mathbf{5}})^I U_{I\,i}\, \Psi_R^i + y\,c_2 f\,(\overline{Q}_L^{\mathbf{5}})^I U_{I\,5}\, t_R + \text{h.c.} \right], \quad (2.7)$$

where $c_{1,2}$ are coefficients expected to be of order 1. The above Lagrangian with totally composite t_R was first written in ref. [18]. Notice the presence of the $\slashed{e} = e_\mu \gamma^\mu$ term which accompanies the derivative of the top partner field: it reconstructs the CCWZ covariant derivative defined in eq. (A.24) and is essential to respect SO(5). In the second line of the equation above we find, first of all, a *direct* interaction, not mediated by the coupling y, among the composite t_R and the top partners. This term is entirely generated by the strong sector and would have been suppressed in the case of partial t_R compositeness. It delivers, looking at the explicit form of d_μ in eq. (A.19), couplings involving the top, the partners and the SM gauge fields. These will play an important role in the single production and in the decay of the top partners. The last two terms give rise, in particular, to the top quark mass but also to trilinear couplings contributing to the single production of top partners. Notice that the indices of the embedding $Q_L^{\mathbf{5}}$ *can not* be contracted directly with those of Ψ because they live in different spaces. The embeddings transform linearly under SO(5) as reported in eq. (2.3) while Ψ transforms under the non-linear representation h. For this reason one insertion of the Goldstone matrix, transforming according to eq. (A.7), is needed.

For brevity we omitted from eq. (2.7) the kinetic term of the gauge fields and of the Goldstone Higgs, the latter is given for reference in eq. (A.21). Moreover we have not yet specified the covariant derivatives D_μ associated with the SM gauge group, these are obviously given by

$$D_\mu q_L = \left(\partial_\mu - igW_\mu^i \frac{\sigma^i}{2} - i\frac{1}{6}g'B_\mu - i\,g_S G_\mu \right) q_L, \quad (2.8)$$

$$D_\mu t_R = \left(\partial_\mu - i\frac{2}{3}g'B_\mu - i\,g_S G_\mu \right) t_R, \quad (2.9)$$

$$D_\mu \Psi = \left(\partial_\mu - i\frac{2}{3}g'B_\mu - i\,g_S G_\mu \right) \Psi. \quad (2.10)$$

where g, g' and g_S are the $\mathrm{SU}(2)_L \times \mathrm{U}(1)_Y$ and $\mathrm{SU}(3)_c$ gauge couplings. We remind the reader that the top partners form a color triplet, hence the gluon in the above equation.

The Lagrangian is very similar for model $\mathbf{M4}_{14}$, where the q_L is embedded in the symmetric traceless $Q_L^{\mathbf{14}}$. We have

$$\mathcal{L}^{\mathbf{M4}_{14}} = i\,\bar{q}_L \slashed{D}\, q_L + i\,\bar{t}_R \slashed{D}\, t_R + i\,\bar{\Psi}(\slashed{D} + i\slashed{e})\Psi - M_\Psi \bar{\Psi}\Psi \quad (2.11)$$
$$+ \left[i\,c_1 \left(\bar{\Psi}_R\right)_i \gamma^\mu d_\mu^i\, t_R + yf\,(\overline{Q}_L^{\mathbf{14}})^{I\,J} U_{I\,i} U_{J\,5}\, \Psi_R^i + \frac{yc_2}{2} f(\overline{Q}_L^{\mathbf{14}})^{I\,J} U_{I\,5} U_{J\,5}\, t_R + \text{h.c.} \right],$$

notice that the two indices of $Q_L^{\mathbf{14}}$ are symmetric and therefore the term that mixes it with Ψ is unique. The factor $\frac{1}{2}$ introduced in the last term is merely conventional.

In both models $\mathbf{M4}_5$ and $\mathbf{M4}_{14}$ the leading order Lagrangian contains four parameters, $\{M_\psi, y, c_1, c_2\}$, on top of the Goldstone decay constant f. One parameter will however have to be fixed to reproduce the correct top mass, while the remaining three parameters could be traded for two physical masses, for instance $m_{X_{5/3}}$ and m_B, and the coupling c_1. It will often be convenient to associate the mass M_Ψ with a coupling g_ψ

$$g_\Psi \equiv \frac{M_\Psi}{f}\,.$$

We will see below that $c_1 \times g_\Psi$ controls the strength of the interactions between the top partners and the Goldstone bosons at energy $\sim M_\Psi$. In particular it controls the on-shell couplings relevant for single production and for two body decays. Notice that, as a function of energy, the effective strength of this trilinear interaction is instead $\sim c_1 E/f$. For $c_1 = O(1)$, as suggested by power counting, the effective coupling is of order $g_* \equiv m_*/f$ at the energy scale of the heavier resonances, in accord with the principle of partial UV completion proposed in ref. [10]. Power counting and partial UV completion then equivalently imply $c_1 = O(1)$ and therefore $c_1 g_\Psi < g_*$. This result obviously follows from the fact that the Higgs is a derivatively coupled pNGB. It would be lost if the Higgs was instead treated as a generic resonance. In the latter case the expected coupling would be independent of the mass and it would be larger, of order g_*. Moreover notice that, although on shell it leads to an effective Yukawa vertex, the interaction associated with c_1 does not affect the spectrum when H acquires a vacuuum expectation value. That again would not be true if we did not account for the pNGB nature of H. The pNGB nature of H is not accounted for in the first thorough work on simplified top partner models [21] and in the following studies (see in particular [22, 28]).

Notice that, a priori, one of the four parameters describing the simplified model could be complex. This is because we have at our disposal only 3 chiral rotations to eliminate the phases from the Lagrangians (2.7) and (2.11). Nevertheless we are entitled to keep all the parameters real if we demand the strong sector respects a CP symmetry defined in appendix A. It is easy to check that CP requires the non-derivative couplings to be real while the coefficient of the term involving to d_μ must be purely imaginary. CP conservations is an additional hypothesis of our construction, however the broad phenomenology does not significantly depend on it.

2.1.2 Top partners in the singlet

The Lagrangian is even simpler if the top partners are in the $\mathbf{1}_{2/3}$. In this case we only have one exotic top-like state which we denote as $\widetilde{T}$. For the two models, $\mathbf{M1}_5$ and $\mathbf{M1}_{14}$ that we aim to consider the Lagrangian reads, respectively

$$\begin{aligned}
\mathscr{L}^{\mathbf{M1}_5} &= \bar{q}_L\, i\slashed{D}\, q_L + \bar{t}_R\, i\slashed{D}\, t_R + i\bar{\Psi}i\slashed{D}\Psi - M_\Psi\bar{\Psi}\Psi \\
&\quad + \left[yf\,(\overline{Q}_L^{\mathbf{5}})^I U_{I\,5}\Psi_R + y\,c_2 f\,(\overline{Q}_L^{\mathbf{5}})^I U_{I\,5}\,t_R + \text{h.c.} \right], \\
\mathscr{L}^{\mathbf{M1}_{14}} &= \bar{q}_L\, i\slashed{D}\, q_L + \bar{t}_R\, i\slashed{D}\, t_R + i\bar{\Psi}i\slashed{D}\Psi - M_\Psi\bar{\Psi}\Psi \\
&\quad + \left[\frac{y}{2}f\,(\overline{Q}_L^{\mathbf{14}})^{I\,J} U_{I\,5}U_{J\,5}\Psi_R + \frac{y\,c_2}{2}f\,(\overline{Q}_L^{\mathbf{14}})^{I\,J}U_{I\,5}U_{J\,5}\,t_R + \text{h.c.} \right].
\end{aligned} \quad (2.12)$$

Notice that we could have also written a direct mixing among t_R and Ψ because the two fields now have identical quantum numbers. However this mixing can obviously be removed by a field redefinition. Models $\mathbf{M1}_5$ and $\mathbf{M1}_{14}$, apart from f, contain three parameters, $\{M_\psi, y, c_2\}$, one of which must again be fixed to reproduce the top mass. We are left with two free parameters that correspond to the coupling c_2 and to the mass $m_{\widetilde{T}}$ of the partners. Notice that in this case all the parameters can be made real by chiral rotations without need of imposing the CP symmetry. The latter symmetry is automatically respected in models $\mathbf{M1}_5$ and $\mathbf{M1}_{14}$.

In order to complete the definition of our models let us discuss the theoretically expected size of their parameters. From the discussion in the introduction and from experience with concrete models, one can reasonably argue that the favorite range for M_Ψ is between $500\,\mathrm{GeV}$ and $1.5\,\mathrm{TeV}$, while g_Ψ is favored in the range $1 \lesssim g_\Psi \lesssim 3$. It is also worth recalling the favorite range of the decay constant $f \equiv M_\Psi/g_\Psi$, which is conveniently traded for the parameter ξ defined in ref. [3]

$$\xi = \frac{v^2}{f^2}\,,\tag{2.13}$$

where $v = 2m_W/g = 246\,\mathrm{GeV}$ is the EWSB scale. Since ξ controls the deviation from the SM at low energies it cannot be too large. Electroweak precision tests suggest $\xi \simeq 0.2$ or $\xi \simeq 0.1$, which corresponds to $f \simeq 500\,\mathrm{GeV}$ or $f \simeq 800\,\mathrm{GeV}$. Smaller values of ξ would of course require more tuning. Finally, the strength of the elementary-composite coupling y is fixed by the need of reproducing the correct mass of the top quark. We will see in the following section that this implies $y \sim y_t = 1$.

2.2 A first look at the models

Now that the models are defined let us start discussing their implications. The simplest aspects will be examined in the present section while a more detailed analysis of their phenomenology will be postponed to the following one.

2.2.1 The spectrum

We start from model $\mathbf{M4}_5$ and we first focus on the fermionic spectrum. The mass-matrix after EWSB is easily computed form eqs. (2.7) and (2.2) by using the explicit form of U on the Higgs VEV obtained from eq. (A.12). By restricting to the sector of 2/3-charged states we find

$$\begin{pmatrix} \bar{t}_L \\ \bar{T}_L \\ \overline{X}_{2/3\,L} \end{pmatrix}^T \begin{pmatrix} -\frac{c_2 y f}{\sqrt{2}}\sin\epsilon & y f \cos^2\frac{\epsilon}{2} & y f \sin^2\frac{\epsilon}{2} \\ 0 & -M_\psi & 0 \\ 0 & 0 & -M_\psi \end{pmatrix} \begin{pmatrix} t_R \\ T_R \\ X_{2/3\,R} \end{pmatrix}\,,\tag{2.14}$$

where $\epsilon = \langle h \rangle/f$ is defined as the ratio among the VEV of the Higgs field and the Goldstone decay constant. The relation among $\langle h \rangle$ and the EWSB scale is reported in eq. (A.23), from which we derive

$$\xi = \frac{v^2}{f^2} = \sin^2\epsilon\,.\tag{2.15}$$

We immediately notice a remarkable feature of the mass-matrix (2.14): only the *first line*, i.e. the terms which involve the t_L, is sensitive to EWSB while the rest of the matrix remains unperturbed. This is due to the fact that the Higgs is a pNGB and therefore its non-derivative interactions can only originate from the breaking of the Goldstone symmetry SO(5). The SO(5) invariant terms just produce derivative couplings of the Higgs and therefore they cannot contribute to the mass-matrix. Since the Goldstone symmetry is broken exclusively by the terms involving the elementary q_L it is obvious that the mass-matrix must have the form of eq. (2.14). Notice that this structure would have been lost if we had not taken into account the pNGB nature of the Higgs. Indeed if we had treated the Higgs as a generic composite SO(4) fourplet, Yukawa-like couplings of order g_* and involving t_R and Ψ would have been allowed. After EWSB those terms would have given rise to $(2,1)$ and $(3,1)$ mass matrix entries of order $g_* v$.

The peculiar structure of the mass-matrix has an interesting consequence. It implies that only one linear combination of T and $X_{2/3}$, with coefficients proportional to the $(1,2)$ and $(1,3)$ entries, mixes with the q_L, while the orthogonal combination does not mix either with the q_L or with any other state. Explicitly, the two combinations are

$$
\begin{aligned}
T' &= \frac{1}{\sqrt{\cos^4 \frac{\epsilon}{2} + \sin^4 \frac{\epsilon}{2}}} \left[\cos^2 \frac{\epsilon}{2} T + \sin^2 \frac{\epsilon}{2} X_{2/3} \right] , \\
X_{2/3}' &= \frac{1}{\sqrt{\cos^4 \frac{\epsilon}{2} + \sin^4 \frac{\epsilon}{2}}} \left[\cos^2 \frac{\epsilon}{2} X_{2/3} - \sin^2 \frac{\epsilon}{2} T \right] .
\end{aligned}
\tag{2.16}
$$

After this field redefinition the mass-matrix becomes block-diagonal

$$
\begin{pmatrix} \bar{t}_L \\ \overline{T}'_L \\ \overline{X}'_{2/3 L} \end{pmatrix}^T
\begin{pmatrix} -\frac{c_2 y f}{\sqrt{2}} \sin \epsilon & y f \sqrt{\cos^4 \frac{\epsilon}{2} + \sin^4 \frac{\epsilon}{2}} & 0 \\ 0 & -M_\psi & 0 \\ 0 & 0 & -M_\psi \end{pmatrix}
\begin{pmatrix} t_R \\ T'_R \\ X'_{2/3 R} \end{pmatrix} ,
\tag{2.17}
$$

so that the state $X'_{2/3}$ is already a mass eigenstate with mass $m_{X_{2/3}} = M_\Psi$. But the spectrum also contains a second particle with exactly the same mass. Indeed the $X_{5/3}$ cannot mix because it is the only state with exotic charge and therefore it maintains the mass $m_{X_{5/3}} = M_\Psi$ it had before EWSB. The $X_{2/3}$ and the $X_{5/3}$ are thus *exactly degenerate*. This remarkable property is due to the pNGB nature of the Higgs and it would be generically violated, as previously discussed, if this assumption was relaxed. This result also depends on t_R being a composite singlet. If t_R was instead a partially composite state mixing to a non-trivial representation of SO(5) (for instance a **5**) there would be additional entries in the mass matrix.[8] In a sense our result depends on y being the only relevant parameter that breaks SO(5) explicitly.

Once the mass-matrix has been put in the block-diagonal form of eq. (2.17) it is straightforward to diagonalize it and to obtain exact formulae for the rotation matrices and for the masses of the top and of the T partner. However the resulting expressions are

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[8]The top partner's spectrum with partially composite t_R has been worked out in ref. [12, 16].
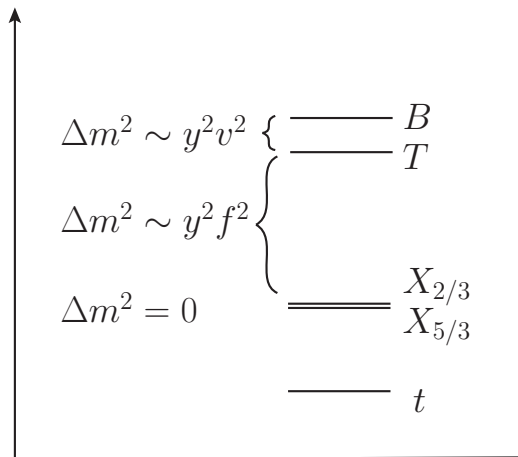
Figure 2. The typical spectrum of the top partners.

rather involved and we just report here approximate expressions for the masses. We have

$$m_t \simeq \frac{c_2 y\, f}{\sqrt{2}} \frac{g_\Psi}{\sqrt{g_\Psi^2 + y^2}} \sin\epsilon \left[1 + \mathcal{O}\left(\frac{y^2}{g_\Psi^2}\xi\right)\right] ,$$

$$m_T \simeq \sqrt{M_\Psi^2 + y^2 f^2} \left[1 - \frac{y^2\left(g_\Psi^2 + (1-c_2^2)y^2\right)}{4\left(g_\Psi^2 + y^2\right)^2} \sin^2\epsilon + \dots\right] . \tag{2.18}$$

From the above equation we obtain the correct order of magnitude for the top mass if, as anticipated, $y \sim y_t$ and $g_\Psi \gtrsim 1$. In this region of the parameter space the corrections to the approximate formulae are rather small, being suppressed by both a factor y^2/g_Ψ^2 (which is preferentially smaller than one) and by $\xi \ll 1$. However we will consider departures from this theoretically expected region and therefore we will need to use the exact formulae in the following sections.

Similarly we can study the sector of $-1/3$ charge states. It contains a massless b_L, because we are not including the b_R in our model, plus the heavy B particle with a mass

$$m_B = \sqrt{M_\Psi^2 + y^2 f^2} . \tag{2.19}$$

This formula is exact and shows that the bottom sector does not receive, in this model, any contribution from EWSB. By comparing the equation above with the previous one we find that the splitting among T and B is typically small

$$m_B^2 - m_T^2 \simeq y^2 f^2 \frac{g_\Psi^2 + (1-c_2^2)y^2}{2\left(g_\Psi^2 + y^2\right)} \sin^2\epsilon , \tag{2.20}$$

and positive in the preferred region $g_\Psi > y$, although there are points in the parameter space where the ordering $m_T > m_B$ can occur. The splitting among the two doublets is instead always positive, $m_B^2 - m_{X_{5/3}}^2 = y^2 f^2$. The typical spectrum of the top partners that we have in our model is depicted in figure 2.

The situation is not much different in model $\mathbf{M4}_{14}$. The mass-matrix for charge 2/3 states has again the form of eq. (2.14)

$$
\begin{pmatrix} \bar{t}_L \\ \bar{T}_L \\ \overline{X}_{2/3\,L} \end{pmatrix}^T
\begin{pmatrix}
-\frac{c_2 y f}{2\sqrt{2}} \sin 2\epsilon & \frac{y f}{2} \left(\cos \epsilon + \cos 2\epsilon \right) & \frac{y f}{2} \left(\cos \epsilon - \cos 2\epsilon \right) \\
0 & -M_\psi & 0 \\
0 & 0 & -M_\psi
\end{pmatrix}
\begin{pmatrix} t_R \\ T_R \\ X_{2/3\,R} \end{pmatrix} , \quad (2.21)
$$

and again it can be put in a block-diagonal form by a rotation among the T and the $X_{2/3}$ similar to the one in eq. (2.16). Therefore also in model $\mathbf{M4}_{14}$ the physical $X_{2/3}$ has mass M_Ψ and it is degenerate with the $X_{5/3}$. The approximate top and T mass are given in this case by

$$
m_t \simeq \frac{c_2 y f}{\sqrt{2}} \frac{g_\Psi}{\sqrt{g_\Psi^2 + y^2}} \frac{\sin 2\epsilon}{2} \left[1 + \mathcal{O}\left(\frac{y^2}{g_\Psi^2} \xi \right) \right] ,
$$

$$
m_T \simeq \sqrt{M_\Psi^2 + y^2 f^2} \left[1 - \frac{y^2 \left(5 g_\Psi^2 + (5 - c_2^2) y^2 \right)}{4 \left(g_\Psi^2 + y^2 \right)^2} \sin^2 \epsilon \right] . \quad (2.22)
$$

Similarly we can compute the mass of the B partner and we find

$$
m_B = \sqrt{M_\Psi^2 + y^2 f^2 \cos^2 \epsilon} \simeq \sqrt{M_\Psi^2 + y^2 f^2} - \frac{y^2 f^2}{2 \sqrt{M_\Psi^2 + y^2 f^2}} \sin^2 \epsilon . \quad (2.23)
$$

In this case, differently from model $\mathbf{M4}_5$ (see eq. (2.19)), the mass of the B is sensitive to EWSB. Apart from this little difference the spectrum is very similar to the one of model $\mathbf{M4}_{14}$ described in figure 2.

The models with the singlet are much simpler because there is only one exotic state. The mass matrices read:

$$
\begin{pmatrix} \bar{t}_L \\ \bar{\widetilde{T}}_L \end{pmatrix}^T
\begin{pmatrix}
-\frac{c_2 y f}{\sqrt{2}} \sin \epsilon & -\frac{y f}{\sqrt{2}} \sin \epsilon \\
0 & -M_\psi
\end{pmatrix}
\begin{pmatrix} t_R \\ \widetilde{T}_R \end{pmatrix} , \quad (2.24)
$$

$$
\begin{pmatrix} \bar{t}_L \\ \bar{\widetilde{T}}_L \end{pmatrix}^T
\begin{pmatrix}
-\frac{c_2 y f}{2\sqrt{2}} \sin 2\epsilon & -\frac{y f}{2\sqrt{2}} \sin 2\epsilon \\
0 & -M_\psi
\end{pmatrix}
\begin{pmatrix} t_R \\ \widetilde{T}_R \end{pmatrix} , \quad (2.25)
$$

for models $\mathbf{M1}_5$ and $\mathbf{M1}_{14}$ respectively. The mass eigenvalues for model $\mathbf{M1}_5$ are

$$
m_t \simeq \frac{c_2 y f}{\sqrt{2}} \sin \epsilon \left[1 + \mathcal{O}\left(\frac{y^2}{g_\Psi^2} \xi \right) \right] ,
$$

$$
m_{\widetilde{T}} \simeq M_\Psi \left[1 + \frac{y^2}{4 g_\Psi^2} \sin^2 \epsilon \right] . \quad (2.26)
$$

For model $\mathbf{M1}_{14}$ instead we have

$$
m_t \simeq \frac{c_2 y f}{2\sqrt{2}} \sin 2\epsilon \left[1 + \mathcal{O}\left(\frac{y^2}{g_\Psi^2} \xi \right) \right] ,
$$

$$
m_{\widetilde{T}} \simeq M_\Psi \left[1 + \frac{y^2}{4 g_\Psi^2} \sin^2 \epsilon \right] . \quad (2.27)
$$

As one can see from the last expressions the mass of the $\widetilde{T}$ receives positive contributions proportional to y^2 and hence for a fixed mass of the $\widetilde{T}$, y must be limited from above. Unlike the models with fourplet partners, in the singlet case y completely controls the couplings of the $\widetilde{T}$ with the top and bottom quarks (see section 3.2). Therefore one can expect that for a given $m_{\widetilde{T}}$ there exists a maximal allowed coupling of the SM particles with the top partner and hence for small masses the single production of $\widetilde{T}$ is suppressed. In addition small values of $m_{\widetilde{T}}$ become unnatural since they require very small y together with a very large c_2 needed to recover correct top mass. By minimizing the largest eigenvalue of the mass matrix with respect to M_Ψ for fixed y and f one can find a minimal allowed mass of the $\widetilde{T}$ which is given by

$$m_{\widetilde{T}}^{\mathrm{min, \, \mathbf{M1}_5}} = m_t + \frac{1}{\sqrt{2}} y f \sin \epsilon \,,$$

$$m_{\widetilde{T}}^{\mathrm{min, \, \mathbf{M1}_{14}}} = m_t + \frac{1}{2\sqrt{2}} y f \sin 2\epsilon \,, \qquad (2.28)$$

for the models $\mathbf{M1}_5$ and $\mathbf{M1}_{14}$ respectively. The bound given in eq. (2.28) will affect the exclusion plots in the following.

2.2.2 Trilinear couplings

Other interesting qualitative aspects of our models are discovered by inspecting the explicit form of the Lagrangians in unitary gauge. These are reported in appendix B, and are written in the "original" field basis used to define the Lagrangians in eqs. (2.5), (2.7), (2.11), (2.12), i.e. before the rotation to the mass eigenstates. Appendix B contains, for reference, the complete Lagrangian including all the non-linear and the derivative Higgs interactions. However the coupling that are relevant to the present discussion are the trilinears involving the gauge fields and the Higgs in the models $\mathbf{M4}_5$ and $\mathbf{M4}_{14}$, reported in eq. (B.1), (B.2), (B.3) and (B.4).

The first remarkable feature of eq. (B.2) is that the Z boson couplings with the B is completely standard: it is not modified by EWSB effects and coincides with the familiar SM expression $g_Z = g/c_w(T_L^3 - Q)$. In particular it coincides with the $Z\bar{b}_L b_L$ coupling, involving the elementary b_L, because b_L and B have the same SU(2) × U(1) quantum numbers. The Z-boson coupling to charge $-1/3$ quarks is therefore proportional to the identity matrix. Consequently the Z interactions remain diagonal and canonical even after rotating to the mass eigenbasis. In particular, in the charge $-1/3$ sector, there will not be a neutral current vertex of the form $B \to Zb$.

This property is due to an accidental parity, P_{LR}, defined in ref. [10] as the exchange of the Left and the Right SO(4) generators. This symmetry is an element of O(4) and it acts on the top partner fourplet of eq. (2.5) and on the Higgs field $\vec{\Pi}$ through the 4×4 matrix

$$P_{LR}^{(4)} = \begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \,. \qquad (2.29)$$

The action of P_{LR} is readily uplifted to O(5) with the 5×5 matrix $P_{LR}^{(5)} = \text{diag}(-1, -1, -1, 1, 1)$. We see that P_{LR} is not broken by the Higgs VEV, which only appears in the last component of the $\vec{\Pi}$ vector. In ref. [26], it was shown that P_{LR} invariance protects the Z couplings from tree-level corrections at zero momentum transfer. That case applied to b quarks, but the statement generalizes straighforwardly: if all the particles with a given charge have the same P_{LR}, then, at tree level in the weak interactions, the neutral current vertices in that charge sector are canonical and, in particular, diagonal.

The Lagrangians (2.7) and (2.11) are approximately P_{LR} invariant, with the breaking coming only from the weak gauge couplings and from the weak mixing y between elementary and composites. However at tree level, for which case the elementary fields can be treated as external spectators, even this weak breaking is ineffective in the charge $-1/3$ and $5/3$ sectors. Notice indeed that according to eqs. (2.5), (2.29), under P_{LR}, B and $X_{5/3}$ are odd, while T and $-X_{2/3}$ are interchanged. Then, inspection of the embedding in eq. (2.2) shows that while we cannot assign a consistent P_{LR} to t_L, we can instead assign negative P_{LR} to b_L. At tree level, t_L will not affect processes involving only quarks with charge $-1/3$ and $5/3$, and therefore the associated explicit breaking of P_{LR} will be ineffective. Analogously the breaking in the gauge sector is seen not to matter at tree level. For a detailed discussion we refer the reader to section 2.4 of ref. [27]. This explains the result previously mentioned for the (b, B) sector and also predicts that the coupling of the $X_{5/3}$ must be canonical as well. This is indeed what we see in eq. (B.2).

The same argument applies to $\widetilde{T}_R$ and t_R in the singlet models $\mathbf{M1}_5$ and $\mathbf{M1}_{14}$. The Z-vertex of those states is not modified, in particular there is no $\bar{t}_R Z \widetilde{T}_R$ vertex and the production/decay with Z is always controlled by left-handed coupling. On the other hand, for $\widetilde{T}_L$ and t_L the argument does not apply, regardless of P_{LR}, given $\widetilde{T}_L$ and t_L do not have the same $\text{SU}(2) \times \text{U}(1)$ quantum numbers.

Another interesting property concerns the W couplings of the B with the charge $2/3$ states. We see in eq. (B.2) that the linear combination of the T and the $X_{2/3}$ that couples with the B is exactly orthogonal to the physical (mass-eigenstate) $X_{2/3}'$ field defined in eq. (2.16) for model $\mathbf{M4}_5$. Only the T' couples to $W B$, leading after the second rotation to transitions among the physical t, T and b, B. Such couplings are instead absent for the physical $X_{2/3}$ which therefore, cannot decay to Wb. This feature is not, for what we can say, the result of a symmetry, but rather an accidental feature of model $\mathbf{M4}_5$. In model $\mathbf{M4}_{14}$ instead the coupling is allowed because the physical $X_{2/3}$ (see the mass-matrix in eq. (2.21)) is not anymore orthogonal to the combination that couples to $W B$. Nevertheless the $X_{2/3}$-B coupling is suppressed by $\langle h \rangle^2 / f^2$ and therefore the decay $X_{2/3} \to Wb$, though allowed in principle, is phenomenologically irrelevant as we will discuss in the following section.

A final comment concerns the couplings of the physical Higgs field ρ. The couplings from the strong sector are only due to the d_μ term in eq. (B.1) and are purely derivative. Therefore, because of charge conservation, they cannot involve the B partner. Higgs couplings in the $-1/3$ charge sector could only emerge from the elementary-composite mixings. However they are accidentally absent in model $\mathbf{M4}_5$, as shown by eq. (B.3). Therefore the decay of the B to the Higgs is absent in this model. In model $\mathbf{M4}_{14}$, on the contrary, this decay is allowed through the vertex in eq. (B.4).

3 Top partners phenomenology

Let us now turn to discuss the main production mechanisms and decay channels of the top partners in the models under consideration. We will first of all, in section 3.1, describe how the cross-sections of the production processes and the partial decay widths can be conveniently parametrized analytically in terms of few universal functions, extracted from the Monte Carlo integration. This method, supplemented with tree-level event simulations to compute the acceptances associated with the specific cuts of each experimental search, will allow us to explore efficiently the multi-dimensional parameter space of our model avoiding a time-consuming scan. Not all the production and decay processes that could be computed with this method are equally sizable, however. In section 3.2 we will present an estimate of the various processes based on the use of the Goldstone boson Equivalence Theorem [29–31], this will allow us to classify (in section 3.3) the channels which are more promising for the search of the top partners at the LHC.

3.1 Production and decay

Given that the partners are colored they can be produced in pairs through the QCD interactions. The pair production cross-section is universal for all the partners and it can be parametrized by a function

$$\sigma_{\text{pair}}(m_X), \tag{3.1}$$

which depends uniquely on the partner's mass m_X, for which we have analytical formulae. We have constructed σ_{pair} by interpolation using the HATHOR code [32] which incorporates perturbative QCD corrections up to NNLO. The values of the cross-section used in the fit are reported in table 2 for the LHC at 7 and 8 TeV center of mass energy. In this and all the other simulations we adopted the set of parton distribution functions MSTW2008 [33].

The other relevant process is the single production of the top partners in association with either a top or a bottom quark. This originates, as depicted in figure 3, from a virtual EW boson $V = \{W^{\pm}, Z\}$ emitted from a quark line which interacts with a gluon producing the top partner and one third-family anti-quark. The possible relevance of single production was first pointed out in ref. [34] . The relevant couplings have the form

$$g_{Xt_R}\overline{X}_R \slashed{V} t_R + g_{Xt_L}\overline{X}_L \slashed{V} t_L + g_{Xb_L}\overline{X}_L \slashed{V} b_L, \tag{3.2}$$

where $X = \{T, B, X_{2/3}, X_{5/3}, \widetilde{T}\}$ denotes generically any of the top partners. At each vertex the EW boson V is understood to be the one of appropriate electric charge. Notice that there is no vertex with the b_R because the latter state is completely decoupled in our model, we expect this coupling to be negligible even in more complete constructions.

It is important to outline that the couplings g_{Xt_R}, g_{Xt_L} and g_{Xb_L} can be computed analytically in our models. They arise from the interactions reported in appendix B after performing the rotation to the physical basis of mass eigenstates. Since the rotation matrices can be expressed in a closed form the explicit formulae for the couplings are straightforwardly derived. The result is rather involved and for this reason it will not be reported here, however it is easily implemented in a *Mathematica* package.

	σ [fb] @ NNLO	
	pair production	
M [GeV]	$\sqrt{s} = 7\,\text{TeV}$	$\sqrt{s} = 8\,\text{TeV}$
400	(0.920) 1.41 $\times 10^3$	(1.50) 2.30 $\times 10^3$
500	(218) 330	(378) 570
600	(61.0) 92.3	(113) 170
700	(19.1) 29.0	(37.9) 56.9
800	(6.47) 9.88	(13.8) 20.8
900	(2.30) 3.55	(5.33) 8.07
1000	(0.849) 1.33	(2.14) 3.27
1100	(0.319) 0.507	(0.888) 1.37
1200	(0.122) 0.196	(0.375) 0.585
1300	(4.62) 7.60 $\times 10^{-2}$	(0.160) 0.253

Table 2. Cross sections for the NNLO pair production of heavy fermions at $\sqrt{s} = 7, 8\,\text{TeV}$ (the LO values are in brackets), with HATHOR [32].
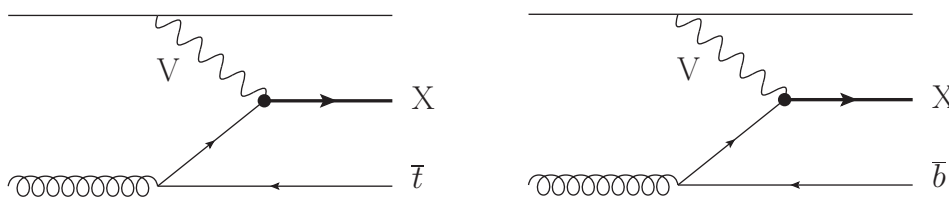
Figure 3. The single-production diagrams.

The single production cross-sections are quadratic polynomials in the couplings, with coefficients that encapsulate the effect of the QCD interactions, the integration over the phase-space and the convolution with the parton distribution functions. These coefficients depend uniquely on the mass of the partner and can be computed by Monte Carlo integration. Once the latter are known we obtain semi-analytical formulae for the cross-sections. The production in association with the $\bar{b}$ is simply proportional to $g^2_{Xb_L}$ while the one with $\bar{t}$ would be, a priori, the sum of three terms proportional to $g^2_{Xt_L}$, $g^2_{Xt_R}$ and $g_{Xt_L} \cdot g_{Xt_R}$ which account, respectively, for the effect of the left-handed coupling, of the right-handed one and of the interference among the two. However in the limit of massless top quark, $m_t \ll m_X$, the processes mediated by the left-handed and by the right-handed couplings become physically distinguishable because the anti-top produced in association with X will have opposite chirality in the two cases. Therefore in the limit $m_t \to 0$ the interference term can be neglected. Moreover, the coefficients of the $g_{Xt_L}{}^2$ and $g_{Xt_R}{}^2$ terms will be equal because the QCD interactions are invariant under parity. Thus the cross-sections

will be very simply parametrized as

$$\sigma_{\text{sing}}(X\overline{t}) = \left[(g_{Xt_L})^2 + (g_{Xt_R})^2\right]\sigma_{Vt}(m_X)\,,$$
$$\sigma_{\text{sing}}(X\overline{b}) = (g_{Xb_L})^2\,\sigma_{Vb}(m_X)\,,$$

(3.3)

in terms of few functions $\sigma_{Vt}(m_X)$ and $\sigma_{Vb}(m_X)$. The charge-conjugate processes, in which either $\overline{X}t$ or $\overline{X}b$ are produced, can be parametrized in terms of a similar set of coefficient functions. The only difference is the charge of the virtual V emitted from the light quark line. We thus have

$$\sigma_{\text{sing}}(\overline{X}t) = \left[(g_{Xt_L})^2 + (g_{Xt_R})^2\right]\sigma_{V^\dagger t}(m_X)\,,$$
$$\sigma_{\text{sing}}(\overline{X}b) = (g_{Xb_L})^2\,\sigma_{V^\dagger b}(m_X)\,,$$

(3.4)

where $V^\dagger$ denotes the charge conjugate of the vector boson V. A similar way of computing cross sections of the $W - b$ fusion type of single-production was carried out in ref. [35] where they adapted the fitting functions of ref. [36] to non-SM couplings.

One might question the validity of the zero top mass approximation which allowed us to neglect the interference and parametrize the cross-section as in eqs. (3.3) and (3.4). We might indeed generically expect relatively large corrections, of the order of m_t/m_X. However the corrections are much smaller in our case, we have checked that they are around 1% in most of the parameter space of our models. The reason is that the interference is further reduced in our case because the left- and right-handed couplings are never comparable, one of the two always dominates over the other. This enhances the leading term, $g_{Xt_L}^2$ or $g_{Xt_R}^2$, in comparison with the interference $g_{Xt_L} \cdot g_{Xt_R}$. Moreover this implies that eqs. (3.3) and (3.4) could be further simplified, in the sum it would be enough to retain the term which is dominant in each case. We will show in the following section that the dominant coupling is g_{Xt_R} in the case of the fourplet (models $\mathbf{M4}_5$ and $\mathbf{M4}_{14}$) and g_{Xt_L} in the case of the singlet (models $\mathbf{M1}_5$ and $\mathbf{M1}_{14}$).

It total, all the single-production processes are parameterized in terms of 5 universal coefficient functions $\sigma_{W^\pm t}$, σ_{Zt} and $\sigma_{W^\pm b}$. Notice that a possible σ_{Zb} vanishes because flavor-changing neutral couplings are forbidden in the charge $-1/3$ sector as explained in the previous section. As such, the single production of the B in association with a bottom quark does not take place. We have computed the coefficient functions $\sigma_{W^\pm t}$ and $\sigma_{W^\pm b}$, including the QCD corrections up to NLO, using the MCFM code [37–40]. To illustrate the results, we report in table 3 the single production cross-section with coupling set to unity, for different values of the heavy fermion mass, and for the 7 and 8 TeV LHC. The values in the table correspond to the sum of the cross sections for producing the heavy fermion and its antiparticle, on the left side we show the results for tB production, on the right one we consider the case of $b\widetilde{T}$. In our parametrization of eqs. (3.3) and (3.4) the cross-sections in the table correspond respectively to $\sigma_{W^+t} + \sigma_{W^-t}$ and to $\sigma_{W^+b} + \sigma_{W^-b}$. We see that the production with the b is one order of magnitude larger than the one with the t, this is not surprising because the t production has a higher kinematical threshold and therefore it is suppressed by the steep fall of the partonic luminosities. The values in

| | σ [pb] @ NLO | | σ [pb] @ NLO | |
| | single production of $\bar{t}B + t\overline{B}$ | | single production of $\bar{b}\widetilde{T} + b\overline{\widetilde{T}}$ | |
M [GeV]	$\sqrt{s} = 7\,\text{TeV}$	$\sqrt{s} = 8\,\text{TeV}$	$\sqrt{s} = 7\,\text{TeV}$	$\sqrt{s} = 8\,\text{TeV}$
400	(2.70) 3.10	(4.32) 4.92	(32.49) 43.47	(47.83) 61.43
500	(1.49) 1.80	(2.50) 2.97	(15.85) 20.44	(24.10) 33.10
600	(0.858) 1.06	(1.49) 1.84	(8.53) 12.89	(13.55) 18.80
700	(0.511) 0.637	(0.928) 1.15	(4.60) 6.70	(7.92) 11.34
800	(0.313) 0.399	(0.590) 0.745	(2.82) 4.01	(4.58) 7.22
900	(0.194) 0.250	(0.377) 0.497	(1.60) 2.50	(2.89) 4.48
1000	(0.121) 0.160	(0.246) 0.325	(0.956) 1.636	(1.81) 2.83
1100	(0.075) 0.103	(0.164) 0.215	(0.604) 0.980	(1.181) 1.72
1200	(0.048) 0.066	(0.107) 0.146	(0.377) 0.586	(0.726) 1.23.
1300	(0.031) 0.043	(0.072) 0.098	(0.234) 0.386	(0.463) 0.731

Table 3. Cross sections for the NLO single production of B and $\tilde{T}$ for a unit coupling, at $\sqrt{s} = 7, 8\,\text{TeV}$ (the LO values are in brackets), with MCFM [37–40].

the table do not yet correspond to the physical single-production cross-sections, they must still be multiplied by the appropriate couplings.

The last coefficient function σ_{Zt} cannot be computed in MCFM and therefore to extract it we used a LO cross section computed with MADGRAPH 5 [41] using the model files produced with FEYNRULES package [42]. To account for QCD corrections in this case we used the k-factors computed with MCFM for the tB production process.

In order to quantify the importance of single production we plot in figure 4 the cross-sections for the various production mechanisms in our models as a function of the mass of the partners and for a typical choice of parameters. We see that the single production rate can be very sizeable and that it dominates over the QCD pair production already at moderately high mass. This is again due to the more favorable lower kinematical threshold, as carefully discussed in ref. [22].

Let us finally discuss the decays of the top partners. The main channels are two-body decays to vector bosons and third-family quarks, mediated by the couplings in eq. (3.2). For the partners of charge 2/3 and −1/3 also the decay to the Higgs boson is allowed, and competitive with the others in some cases. This originates from the interactions of the partners with the Higgs reported in appendix B, after the rotation to the physical basis of mass eigenstates. The relevant couplings can be computed analytically similarly to the $g_{t_{L,R}X}$ and $g_{b_L X}$. Thus we easily obtain analytical tree-level expressions for the partial widths and eventually for the branching fractions. In principle cascade decays $X \to X'V$ or $X'H$ are also allowed, however these are never sizable in our model as we will discuss in section 3.3.
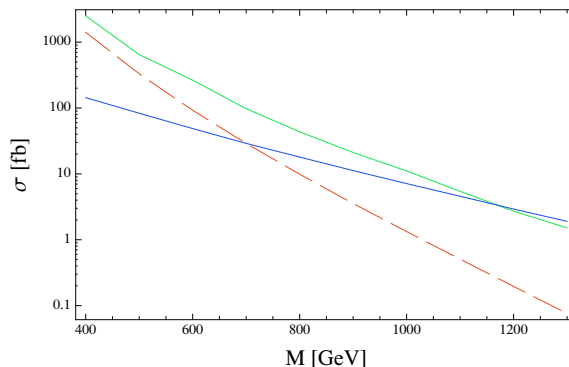
Figure 4. In red dashed: the cross sections of pair production. In green and blue the single production of the $\widetilde{T}$(in association with a b) and of the $X_{5/3}$(in association with a t), respectively in model $\mathbf{M1}_5$ and $\mathbf{M4}_5$. The point chosen in the parameter space is $\xi = 0.2$, $c_1 = 1$ and $y = 1$. The value of c_2 is fixed, at each value of M_Ψ, in order to reproduce the top quark mass.

3.2   Couplings to Goldstone bosons

Let us now turn to classify the relative importance of the various production mechanisms and decay channels described in the previous section. Since the partners are much heavier than the EW bosons, $m_X \gg m_W$, their dynamics is conveniently studied by using the Equivalence Theorem, which applies at energies $E \gg m_W$. To this end, we will momentarily abandon the unitary gauge and describe our model in the R_ξ-gauge where the Goldstone degrees of freedom associated with the unphysical Higgs components are reintroduced. The Higgs field is now parameterized as[9]

$$H = \begin{pmatrix} h_u \\ h_d \end{pmatrix} = \begin{pmatrix} \phi^+ \\ \frac{1}{\sqrt{2}}\left(\langle h \rangle + \rho + i\phi^0\right) \end{pmatrix} . \tag{3.5}$$

The Equivalence Theorem states that, at high energies, the longitudinal components of the $W^\pm$ and of the Z bosons are described, respectively, by the charged and the neutral Goldstone fields $\phi^\pm$ and ϕ^0. The transverse polarizations are instead well described by vector fields $W_\mu^\pm$ and Z_μ, in the absence of symmetry breaking. However the transverse components give a negligible contribution to our processes, and this is for two reasons. First, their interactions emerge from the SM covariant derivatives and therefore these are proportional to the EW couplings g or g'. We will see below that the couplings of the longitudinal, i.e. of the Goldstones, are typically larger than that. Second, the transverse components can not mediate, before EWSB, any transition between particles in different multiplets of the gauge group. Indeed the couplings of the $W_\mu^\pm$ and Z_μ fields are completely fixed by gauge invariance and therefore they are diagonal in flavor space. Only after EWSB do states from different multiplets mix and flavor-changing couplings like in eq. (3.2) arise. Therefore these effects must be suppressed by a power of $\epsilon = \langle h \rangle / f$. This means that the

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[9]Notice that the Goldstone fields $\phi^{\pm,0}$ in eq. (3.5) are not canonically normalized. Indeed the non-linearities in the Higgs kinetic term of eq. (A.21) lead to a kinetic coefficient equal to $\sin \epsilon / \epsilon$, with $\epsilon = \langle h \rangle / f$. However this is irrelevant for the purpose of the present discussion.

transverse gauge bosons basically do not participate to the production and decay of the top partners: the decay will mostly be to longitudinally polarized vectors, while the virtual V exchanged in single production diagram will be dominantly longitudinally polarized.

For our purposes, we can thus simply ignore the vector fields and concentrate on the Goldstones. In the models with the fourplet, $\mathbf{M4}_5$ (2.7) and $\mathbf{M4}_{14}$ (2.11), the first source of Goldstone couplings is the term $i\,c_1\left(\bar{\Psi}_R\right)_i \slashed{d}^i\, t_R$. One would naively expect this interaction to be the dominant one because it originates entirely from the strong sector without paying any insertion of the elementary-composite coupling y. Before EWSB the couplings are

$$i\,\frac{\sqrt{2}c_1}{f}\left[-\overline{T}\gamma^\mu t_R\partial_\mu\left(\frac{\rho-i\phi^0}{\sqrt{2}}\right)+\overline{B}\gamma^\mu t_R\partial_\mu\phi^-+\overline{X}_{2/3}\gamma^\mu t_R\partial_\mu\left(\frac{\rho+i\phi^0}{\sqrt{2}}\right)+\overline{X}_{5/3}\gamma^\mu t_R\partial_\mu\phi^+\right]+\text{h.c.}.\tag{3.6}$$

It is not difficult to check that the interactions above respect not only the SM but also the full SO(4) symmetry of the strong sector. Eq. (3.6) contains derivative operators, therefore it is not yet suited to read out the actual strength of the interactions. However it can be simplified, provided we work at the tree-level order, by making use of the equations of motion of the fermion fields.[10] After integrating by parts and neglecting the top mass, we find

$$\frac{\sqrt{2}c_1}{f}\left[-m_T\left(\frac{\rho-i\phi^0}{\sqrt{2}}\right)\overline{T}t_R+m_B\phi^-\overline{B}t_R+m_{X_{2/3}}\left(\frac{\rho+i\phi^0}{\sqrt{2}}\right)\overline{X}_{2/3}t_R+m_{X_{5/3}}\phi^+\overline{X}_{5/3}t_R\right]+\text{h.c.},\tag{3.7}$$

showing that the strength of the interaction is controlled by the masses of the heavy fermions. Neglecting the elementary-composite coupling y, the masses all equal M_Ψ, and the coupling, modulo an $O(1)$ coefficient, is given by $g_\Psi = M_\Psi/f$, as anticipated in the previous section. Once again we remark that this feature follows from the Goldstone boson nature of the Higgs. Indeed if the Higgs were a generic resonance, not a Goldstone, then it could more plausibly have a Yukawa $g_*\overline{\Psi}^i\Pi_i t_R$ vertex with strength dictated by the strong sector coupling g_*.

Those of eq. (3.7) are the complete Goldstone interactions in the limit of a negligible elementary-composite coupling y. However we can not rely on this approximation because we will often be interested in relatively light top partners, with $g_\Psi \leq y \simeq y_t$. It is straightforward to incorporate the effect of y, due to the mixing terms in eqs. (2.7) and (2.11) for model $\mathbf{M4}_5$ and $\mathbf{M4}_{14}$, respectively. After diagonalizing the mass-matrix, again neglecting

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[10]When considering a perturbation described by a small parameter η to a Lagrangian, the use of the equations of motion of the unperturbed theory is equivalent to permorming field redefinitions of the form $\Phi \to \Phi + \eta F[\Phi,\partial]$. For example, to deal with the first term of eq. (3.6), the relevant redefinition is

$$\begin{aligned}T_R &\to T_R + \frac{\sqrt{2}c_1}{f}h_d^\dagger t_R\\t_R &\to t_R - \frac{\sqrt{2}c_1}{f}h_d T_R\end{aligned}.$$

This eliminates the derivative interaction and makes the first term of eq. (3.7) appear. It also leads to new interactions with more fields that however are irrelevant for our processes at the tree-level.

EWSB, the Goldstone interactions for both models become

	$\mathbf{M4}_5$, $\mathbf{M4}_{14}$
$\phi^+ \overline{X}_{5/3\,L}\, t_R$	$\sqrt{2}c_1 g_\psi$
$(\rho + i\phi^0)\overline{X}_{2/3\,L}\, t_R$	$c_1 g_\psi$
$(\rho - i\phi^0)\overline{T}_L\, t_R$	$-c_1\sqrt{y^2 + g_\psi^2} + \dfrac{c_2 y^2}{\sqrt{2}\sqrt{y^2 + g_\psi^2}}$
$\phi^- \overline{B}_L\, t_R$	$c_1\sqrt{2}\sqrt{y^2 + g_\psi^2} - \dfrac{c_2 y^2}{\sqrt{y^2 + g_\psi^2}}$

$$(3.8)$$

which reduces to eq. (3.7) for $y \ll g_\Psi$. Notice that eq. (3.8) only contains couplings with the right-handed top quark. This is not surprising because the top partners live in SM doublets and therefore their only allowed Yukawa-like interactions are with the t_R singlet. The couplings with the q_L doublet emerge only after EWSB and are suppressed by one power of ϵ. Therefore they typically do not play a mayor role in the phenomenology. Obviously the SM symmetry is respected in eq. (3.8), this explains the $\sqrt{2}$ suppression of the $X_{2/3}$ and of the T couplings compared with the ones of the $X_{5/3}$ and of the B.

The situation is different in the models with the singlet, $\mathbf{M1}_5$ and $\mathbf{M1}_{14}$ (2.12). In that case there is no direct contribution from the strong sector to the Goldstone coupling and all the interactions are mediated by y. The couplings are

	$\mathbf{M1}_5$, $\mathbf{M1}_{14}$
$(\rho + i\phi^0)\overline{\widetilde{T}}_R\, t_L$	$\dfrac{y}{\sqrt{2}}$
$\phi^+ \overline{\widetilde{T}}_R\, b_L$	y

$$(3.9)$$

The top partner $\widetilde{T}$ now is in a SM singlet, therefore the interactions allowed before EWSB are the ones with the left-handed doublet. The $\sqrt{2}$ suppression of the coupling with the top is due, once again, to the SM symmetry. One important implication of eq. (3.9) is that the $\widetilde{T}$, contrary to the partners in the fourplet, can be copiously produced singly in association with a bottom quark. We will discuss this and other features of our models in the following section.

3.3 The most relevant channels

We discuss here the most relevant production and decay processes of each top partner, identifying the best channels where these particles should be looked for at the LHC. Obviously one would need an analysis of the backgrounds to design concrete experimental searches for these promising channels and to establish their practical observability. We leave this to future work and limit ourselves to study, in section 4, the constraints on the top partners that can be inferred from presently available LHC searches of similar particles

Let us first consider the models $\mathbf{M4}_5$, $\mathbf{M4}_{14}$ and analyze separately each of the new fermions.

- **$X_{5/3}$.** $X_{5/3}$, together with $X_{2/3}$, is the lightest top partner, it is therefore the easiest to produce. Production can occur in pair, via QCD interactions, or in association with
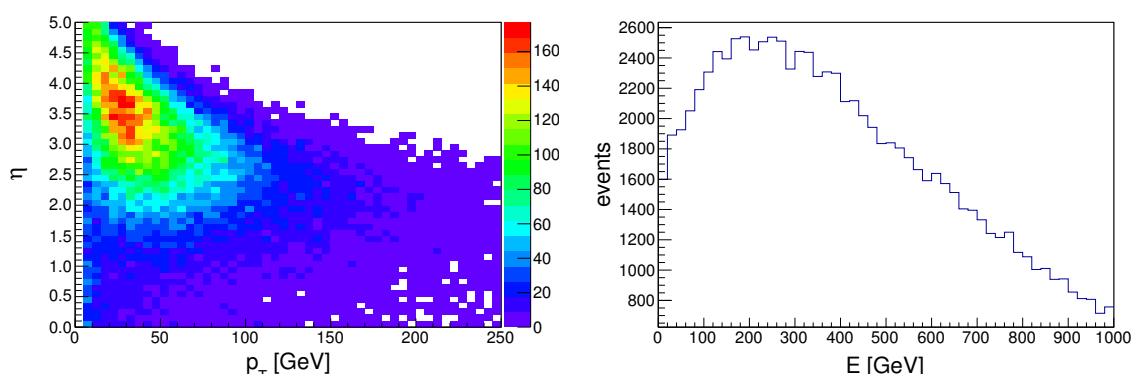
Figure 5. $p_T - \eta$ and energy distributions of the forward jets produced in a single production of the top partner with a mass 600 GeV.

a top quark through its coupling with a top and a W^+. The coupling, see eq. (3.8), is controlled by $g_\psi = m_{X_{5/3}}/f$, which grows with mass at fixed f. We thus expect single production to play an important role at high mass, where it is enhanced with respect to pair production by both kinematics and a larger coupling (at fixed f). This is confirmed, for a particular but typical choice of parameters, by the plot in figure 4.

Since it is the lightest partner, $X_{5/3}$ decays to W^+t with unit branching ratio. The relevant channel for its observation is $X_{5/3} \to tW$ in association with a second top quark of opposite charge. The latter is present in both single and pair production processes. This results in clean signals consisting of either same-sign dileptons or trileptons plus jets. In the following section we will recast the LHC searches for these signals and obtain a limit on $X_{5/3}$ production. In addition to two top quarks and a W, pair production also leads to a second hard W while single production (see figure (3)) features a light-quark jet associated with virtual W emission.

Notice that the light-quark jet in single production is typically forward with a $p_T \lesssim m_W$ because the emission of the virtual W is enhanced in this kinematical region [22]. In practice this jet has the same features of the "tag jets" in VBF Higgs production and in WW-scattering. The events are thus characterized by a forward isolated jet in one of the hemispheres. The relevant kinematical distributions are shown in figure (5) for the production of a 600 GeV partner. Like in VBF or WW-scattering, one might hope to employ the forward jet as a tag to discriminate single production form the background. Ref. [22] argued that the main source of forward jets in the background, QCD initial state radiation, tends to produce more central and less energetic jets, however further investigations are needed. Present LHC searches are designed for pair- rather than for single-production. Because of the η^{jet} and p_T^{jet} cuts that they adopt, they are thus weakly sensitivity to forward jets. We believe that it would be worth to explore the possible relevance of forward jets in designing the searches for top partners.

- **$X_{2/3}$.** $X_{2/3}$ is also light and therefore easier to produce than the heavier partners. At the leading order, as eq. (3.8) shows, it couples with strength $c_1 g_\psi$ to the Higgs and Z bosons. The dominant decay channels are thus $X_{2/3} \to Zt$ and $X_{2/3} \to ht$ and $\mathrm{BR}(X_{2/3} \to Z\,t) \approx \mathrm{BR}(X_{2/3} \to h\,t) \approx 0.5$. In model $\mathbf{M4}_5$ the coupling to Wb vanishes exactly, while in model $\mathbf{M4}_{14}$ the coupling is non-zero but suppressed by $\epsilon \sim v/f$. The decay $X_{2/3} \to Wb$ is therefore typically sub-dominant and can become relevant only in a corner of parameter space characterized by low mass, $y\epsilon = O(1)$ and $c_1 < 1$. Given that $X_{2/3} \to ht$ is probably difficult to detect (see however ref. [43, 44] for recent analyses), the search for $X_{2/3}$ must rely on the decay mode $X_{2/3} \to Zt$, with Z further decaying to charged leptons. An extra suppression from the small branching ratio must then be payed. This disfavors the $X_{2/3}$ signal compared to that of $X_{5/3}$, for which the branching ratio needed to reach the leptonic final state is close to one.

  $X_{2/3}$ is produced in pairs via QCD interactions and singly via the $ZX_{2/3}t$ coupling,. In the latter case a top quark is produced in association. Both production modes lead to a resonant $X_{2/3} \to Zt$ plus one top of opposite charge. In the case of single production there will be a forward jet, as previously discussed in the case of $X_{5/3}$. In the case of pair production there will be either a Higgs or a Z from the other partner. Another possible single production mode, in association with a b quark rather than a t, is strictly forbidden in model $\mathbf{M4}_5$ and is suppressed by the small coupling to Wb in model $\mathbf{M4}_{14}$. However single production in association with a b is kinematically favored over that with t. Kinematics then compensates the suppressed coupling and makes the two rates typically comparable in model $\mathbf{M4}_{14}$, as shown in figure 6. By comparing with figure 4, we see that, in the case of $X_{2/3}$, single production in association with a t is suppressed compared to the case of $X_{5/3}$.[11] This is mainly due to the $\sqrt{2}$ factor in charged current versus neutral current vertices, see eq. (3.8). Moreover, the difference between the W and Z couplings, taking into account u- and the d-type valence quark content of the proton, further enhances by a ~ 1.2 factor the virtual W emission rate with respect to the Z rate. Combining this enhancement with the factor of 2 in the squared coupling, one explains the relative sizes of the $X_{5/3}$ and $X_{2/3}$ production cross sections.

- **T.** T is systematically heavier than $X_{2/3}$, but the phenomenology is very similar. Therefore it will merely give a subdominant contribution to the $X_{2/3}$ channels described in the previous paragraph. Indeed, by eq. (3.8), also T couples at leading order with equal strength to the Higgs and to the Z, leading to $\mathrm{BR}(T \to Z\,t) \approx \mathrm{BR}(T \to h\,t) \approx 0.5$. The coupling to Wb arises at order ϵ, and it can be relevant, as explained for $X_{2/3}$ above, thanks to the favorable kinematics of associated production with a b.

  One may in principle consider chain decays seeded by $T \to X_{2/3}Z$, $T \to X_{2/3}h$ or $T \to X_{5/3}W$, given these channels are normally kinematically open. However the

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[11]Even though the two plots correspond to different models the couplings of the $X_{5/3}$ and $X_{2/3}$ do not differ at leading order in models $\mathbf{M4}_5$ and $\mathbf{M4}_{14}$.
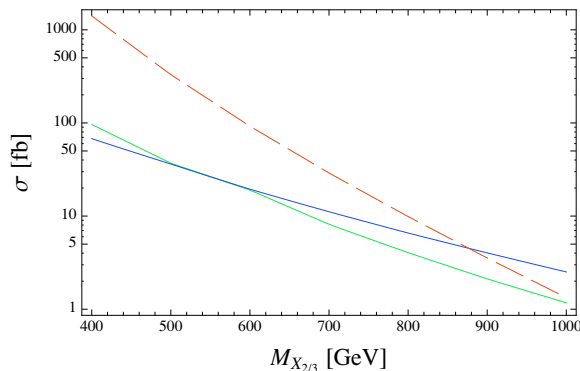
Figure 6. Cross sections of the $X_{2/3}$ pair (red dashed line) and single production in association with a t (blue line) and with a b (green line) for the parameters choice: $y = 1$, $c_1 = 1$, $\xi = 0.2$ in the model $\mathbf{M4}_{14}$.

corresponding couplings are generically smaller than those controlling the direct decays to t_R. This is a straightforward consequence of the equivalence theorem and of SU(2) selection rules. The decays to t_R, involve longitudinally polarized vectors and h, living in the linear Higgs doublet H: given the top partners are SU(2) doublets and t_R is a singlet, the coupling respects SU(2) and so it arises at zeroth order in ϵ. On the other hand, the transitions among top partners living in different SU(2) doublets obviously require an extra insertion of the Higgs vacuum expectation value. The resulting amplitudes are therefore suppressed by one power of ϵ and the corresponding branching ratios negligible.

- **B.** B is even heavier than T, though the mass difference, $m_B - m_T \sim y^2 v^2 / 4 m_B$ (see eq. (2.20)), is typically rather small. The most relevant decay mode is $B \to Wt$, mediated by the coupling $\sim c_1 g_\Psi$ in eq. (3.8). Like in the case of T, SU(2) selection rules suppress the decay to $W X_{2/3}$. Moreover, the decay $B \to WT$, when kinematically allowed, proceeds either via a transverse W, with SM gauge coupling $g < g_\Psi$, or via a longitudinal W, with effective coupling suppressed by ϵ. Therefore also this decay is significantly suppressed. The decay $B \to Zb$ is forbidden because, as we explained in section 2.2.2, flavor-changing neutral couplings are absent in the charge $-1/3$ sector. The $B \to hb$ channel is forbidden in model $\mathbf{M4}_5$ and suppressed by ϵ in model $\mathbf{M4}_{14}$. In the latter model it can play a role, but only in a corner of the parameter space.

  Single production, since the ZBb vertex is absent, is always accompanied by a top quark. The signature of single B production is therefore a resonant $B \to Wt$ plus an opposite charge top, the same final states of single $X_{5/3}$ production. In the end, B production, single and pair, has the same signatures as $X_{5/3}$ production: same sign leptons or trileptons plus jets.

Let us now switch to models $\mathbf{M1}_5$ and $\mathbf{M1}_{14}$, where the only new heavy fermion is the $\tilde{T}$.

- **$\widetilde{T}$.** $\widetilde{T}$ has a very rich phenomenology because it can be copiously produced through all the three mechanisms described above. We see in eq. (3.9) that $\widetilde{T}$ couples to both Zt and Wb, with a coupling of order $y \sim y_t/c_2$. It can therefore be singly produced either in association with a top or with a bottom quark. Notice that in the range $c_2 \sim 1$ suggested by power counting, the trilinear coupling is of order y_t, which is expected to be generically smaller than the strong sector coupling g_ψ that controls the single production of top partners in a $(2,2)$. The bands in the left panel of figure 7, indicate the single prooduction cross section[12] for $0.5 < c_2 < 2$: comparing the blue band to the corresponding case of $X_{2/3}t$ and $X_{5/3}t$ production in models $\mathbf{M4}_5$ and $\mathbf{M4}_{14}$, one notices, as expected, a typically smaller rate for models $\mathbf{M1}_5$ and $\mathbf{M1}_{14}$. While $y \sim y_t$ ($c_2 \sim 1$) is favored by naive power counting, one can entertain the possibility of choosing $y > y_t$ ($c_2 < 1$), for which the single production rate can be sizeable. However, for a given value of $m_{\widetilde{T}}$ and f, there is a mathematical upper bound $y_{\max}$ on y determined by eqs. (2.28). The right plot in figure 7 shows that $y_{\max}$ grows with $m_{\widetilde{T}}$ and that it is comparable in model $\mathbf{M1}_5$ and model $\mathbf{M1}_{14}$. In the left panel of figure 7, the green line and the blue line shows, respectively for $\tilde{T}b$ and $\tilde{T}t$, the maximal allowed cross section, which basically coincides with the choice $y = y_{\max}$.[13] For such maximal values the single production cross section can be quite sizeable.

  Single production of a $\tilde{T}$-like partner was considered in the context of Little Higgs models in refs. [45, 46], and more recently for composite Higgs models in ref. [47], where it was also considered the possibility of using a forward jet tag as a handle for this kind of searches. The total cross section in this channel is favored over single production with a t by both kinematics and by the $\sqrt{2}$ factor in charged current transitions. Indeed, as shown in figure (7) associated $\tilde{T}b$ production dominates even over pair production in all the relevant mass-range while single production with the t is rather small. The role of kinematics is especially important in this result, as the large $\tilde{T}b$ cross section is dominated by the emission of a soft b, with energy in the tens of GeV, a regime obviously unattainable in the similar process wih a t. Indeed by performing a hard cut of order m_t on the p_T of the b, the $\tilde{T}b$ cross section would become comparable to that for $\tilde{T}t$. Unfortunately the current LHC searches do not exploit the large inclusive rate of production with the b quark because they are designed to detect pair production. We will show in the following section that the acceptance of single production, with the cuts presently adopted is extremely low. We believe there is space for substantial improvement in the search strategy.

  Also concerning decays, all the possible channels are important in the case of $\widetilde{T}$. It decays to Wb, Zt and ht at zeroth order in ϵ, with a fixed ratio of couplings. By looking at eq. (3.9) we obtain $\text{BR}(\widetilde{T} \to Zt) \approx \text{BR}(\widetilde{T} \to ht) \approx \frac{1}{2}\text{BR}(\widetilde{T} \to$

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[12]By fixing m_t, ξ, c_2 and $m_{\tilde{T}}$ the result for model $\mathbf{M1}_{14}$ and $\mathbf{M1}_5$ coincide. Indeed, by comparing the lagrangians (B.6) and (B.7), one notices that the gauge vertices and the mass spectrum of model $\mathbf{M1}_{14}$ equal those of model $\mathbf{M1}_5$ when the equality $y^{\mathbf{M1}_5}\sin\epsilon = y^{\mathbf{M1}_{14}}\sin 2\epsilon/2$ holds.

[13]Note that, for a given $m_{\tilde{T}}$, $y_{\max}$ does indeed correspond to the maximal value of the $W\bar{b}\widetilde{T}$-coupling, while the coincidence is not exact in the case of the $Z\bar{t}\widetilde{T}$-coupling.
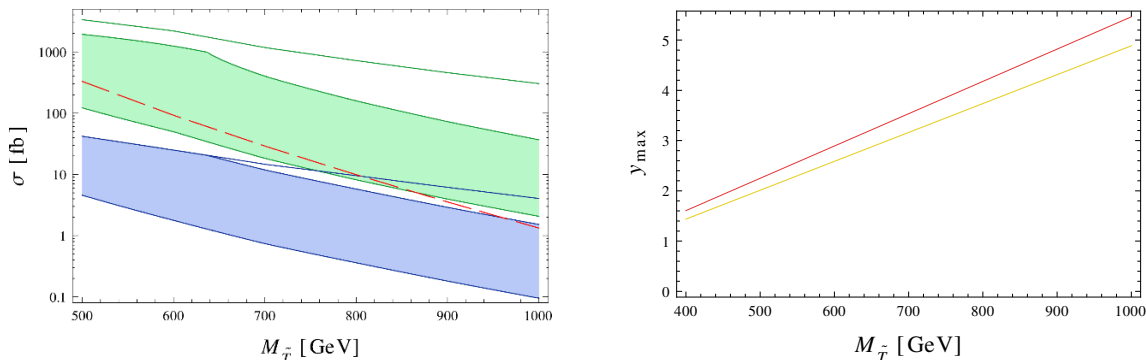
Figure 7. Left panel: cross sections for the different production mechanisms of $\widetilde{T}$ for the models **M1**$_5$ and **M1**$_{14}$ for $\xi = 0.2$. Red dashed: pair production; green line: $\tilde{T}b$ production with the maximal allowed coupling, green band: $\tilde{T}b$ production for $0.5 < c_2 < 2$; blue line: $\tilde{T}t$ production for the maximal allowed coupling, blue band: $\tilde{T}t$ production for $0.5 < c_2 < 2$. Right panel: maximal allowed y for the models **M1**$_5$ (in yellow) and **M1**$_{14}$ (in red).

$W\,b) \approx 0.25$. Actually the branching fraction to Wb is even further enhanced by the larger phase space, though this is only relevant for low values of $m_{\widetilde{T}}$. Given that the branching fraction is larger, ideally the resonant Wb production would be the best channel to detect the $\widetilde{T}$. However one should manage to design a search strategy to reject the background while retaining the signal. In particular one should retain as much as possible the contribution from the large single production in association with the b. A possibly cleaner decay channel could then be $\widetilde{T} \to Z\,t$ with leptonic Z.

4   LHC bounds

In this section we derive bounds on our models using the presently available LHC searches. Given that the top partners are heavy fermions coupled to top and bottom, we focus on the experimental searches for 4th family quarks, which present a somewhat similar phenomenology.[14] We will make use of the following searches for 4th family quarks performed by CMS: 1) $b' \to Wt$ with same-sign dileptons or trileptons in the final state [50]; 2) $t' \to Zt$ with trileptons in the final state [51]; 3) $t' \to Wb$ with two leptons in the final state [52].

In what follows, we quantify the impact of these three searches on our models, by adopting the following strategy. We compute separately the production cross-sections of the top partners, the branching fractions into the relevant channels and the efficiencies associated with the selection cuts performed in each experimental search. The cross-sections and the branching fractions at each point of the parameter space are encapsulated in semi-analytical formulae as described in section 3. The efficiencies must instead be obtained numerically through a Monte Carlo simulation. Not having at our disposal a reliable tool to estimate the response of the detector, a fully realistic simulation of the hadronic final states would not be useful. Therefore we decided not to include showering and hadronization effects in

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[14]Significant bounds on the top partners could also emerge from unrelated studies like the searches of SUSY performed with the "razor" variable [48, 49]. We thank M. Pierini for suggesting this possibility, obviously this is an interesting direction to explore.

our analysis, and we stopped at the parton level. We applied the reconstruction (e.g., of b-jets and leptons) and selection cuts on the partonic events in order to get an estimate of the kinematical acceptance. Moreover, we included the efficiencies for b-tagging, lepton reconstruction and trigger through universal reweighting factors extracted from the experimental papers. In oder to account for the possible merging of soft or collinear partons in single jet we applied the anti-k_T clustering algorithm [53] for jet reconstruction with distance parameter $\Delta R = 0.5$.

4.1 Search for $b' \to W t$

This search applies only to models $\mathbf{M4}_5$, $\mathbf{M4}_{14}$. The analysis of ref. [50] aims at studying a 4th family b' that is pair produced by QCD and is assumed to decay to Wt with unit branching fraction. The search is performed in the final state with at least one tagged b-jet and either same-sign dileptons or trileptons (e or μ). Three or two additional jets are required, respectively, in the dilepton and trilepton channels. Apart from the usual isolation, hardness and centrality cuts for the jets and the leptons, a hard cut is required on the scalar sum of the transverse momenta of the reconstructed object and missing p_T. Ref. [50] reports the observed number of events in the two categories and the expected SM background. From these elements, given the efficiency of the signal in the two channels, one puts a bound on the pair production cross-section and eventually on the mass of the b'. With $4.9\,fb^{-1}$ of data at $7\,\mathrm{TeV}$ the bound is $611\,\mathrm{GeV}$ at 95% confidence level. Below we will quantify the impact of this search on the parameter space of our models.

The top partners contributing to the signal are $X_{5/3}$ and B because, as shown in the previous section, they lead to two tops of opposite charge and to at least one extra W in both pair and single production. To derive the bound we must compute, for each partner and production mode, the efficiency of the signal in the dilepton and the trilepton channels as a function of the partner's mass. The total production cross-sections are computed semi-analytically at each point of the parameter space. Combining the cross-sections with the efficiencies we obtain the signal yield in the two channels that must be compared with the observed number of the events and with the expected background. We perform this comparison by computing the confidence level of exclusion (CL) defined through the CL_s hypothesis test [54], as explained in some detail in appendix C. At the practical level it is important that at the end of this procedure we obtain an *analytical* expression for the CL as a function of the fundamental parameters of our model. This makes very easy and fast to draw the exclusion bounds even if we work in a multi-dimensional parameter space.

Efficiencies

The first step is to simulate the signal processes. Rather than employing our complete model we have used a set of simplified MadGraph models containing the SM fields and interactions plus the two relevant new particles — $X_{5/3}$ and B — with the appropriate couplings to Wt responsible for the single production and the decay. We will employ the right-handed $X_{5/3}Wt_R$ or BWt_R vertices because, as we have shown in section 3.2, the top partners couple mainly to the t_R. However, to make contact with ref. [50], we simulated also the case of left-handed vertices because for a 4th family b' the coupling originates from an off-diagonal entry of the generalized V_{CKM} matrix and it is purely left-handed. We will see that the chirality of the couplings significantly affects the efficiencies.

M [GeV]	$X_{5/3}$ partner [%]	B partner [%]	4th family b' [%]	b' ref. [50] [%]
450	1.90 ± 0.05	1.93 ± 0.05	1.65 ± 0.04	1.52 ± 0.13
550	1.97 ± 0.05	1.98 ± 0.05	1.72 ± 0.05	1.71 ± 0.14
650	1.96 ± 0.05	1.96 ± 0.05	1.85 ± 0.05	1.71 ± 0.15

Table 4. Efficiencies for the pair produced B and $X_{5/3}$ going to same-sign dileptons. Efficiencies contain the cuts losses, b-tagging performance and BR's of W boson.

We generated parton level events without showering, hadronization and detector simulation. The events were analyzed using the cuts and the identification/reconstruction efficiencies for b-tagging and leptons reported in [50]. We also included the trigger efficiency as an overall multiplicative factor. Not having enough information on how the τ leptons were treated in the analysis we have accounted only for the missing energy from the tau decays while the jets and leptons candidates coming from taus were simply rejected. We checked that the inclusion of τ-jets does not introduce appreciable differences, but τ-leptons might affect our results. We have found that the most severe cut is the one on the transverse momenta of the leptons candidates, $p_T > 20$ GeV. This is because most of the events which could contribute to di-(tri-)leptons contain exactly 2(3) charged lepton candidates, thus loosing only one of them causes the loss of the event. The number of generated jets per event is instead larger than the minimally required one and therefore the impact of the jet cut is less prominent.

The signal efficiency is defined as the product of the cut efficiencies with the branching ratios of the t and the W to the required final states. The results are given in tables 4 and 5 for different mass points. In these tables, the efficiencies of the pair-produced b' obtained in ref. [50] are compared with the ones obtained for a left-handed coupling with our method. The accuracy of our simplified treatment of QCD radiation and detector effects is quantified by the level of agreement between these results. We see that the discrepancy is below 10% in the dilepton channel and around 30% in the case of trileptons. In view of these results we have decided to be conservative and to present our results by showing exclusion limits computed using our efficiency and also using an efficiency reduced respectively by 10% for dileptons and 30% for trileptons. From tables 4 and 5 we also see that the efficiency in our model is significantly larger than the one for the 4th family b'. This is because the right-handed top (and the left-handed anti-top) produced in the decay in our models tends to produce more energetic charged leptons than a left-handed top. The lepton p_T distribution is therefore harder and the cut $p_T > 20$ GeV is more easily satisfied. Finally, we notice, somewhat surprisingly, that the efficiencies for the $X_{5/3}$ and for the B partners are substantially identical. One would have expected some difference at least in the dilepton channel, since the two leptons come from the decay of a single heavy particle in the first case while they have a different origin in the second one. However this makes no difference in practice.

Plots and results

Now using the event analysis algorithm shortly described above we can compute the signal efficiencies for same-sign dileptons and trileptons in the framework of the model with

M [GeV]	$X_{5/3}$ partner [%]	B partner [%]	4$^{\text{th}}$ family b' [%]	b' ref. [50] [%]
450	0.88 ± 0.02	0.84 ± 0.02	0.69 ± 0.02	0.47 ± 0.05
550	0.98 ± 0.02	0.94 ± 0.02	0.81 ± 0.02	0.56 ± 0.05
650	1.04 ± 0.03	1.07 ± 0.02	0.82 ± 0.02	0.63 ± 0.06

Table 5. Efficiencies for the pair produced B and $X_{5/3}$ going to trileptons containing two opposite-sign leptons. Efficiencies contain the cuts losses, b-tagging performance and BR's of W boson.

	dilept eff.		trilept eff.	
M[GeV]	for B [%]	for $X_{5/3}$ [%]	for B [%]	for $X_{5/3}$ [%]
400	1.67 ± 0.03	1.61 ± 0.04	0.66 ± 0.01	0.67 ± 0.02
600	1.96 ± 0.03	2.02 ± 0.04	0.93 ± 0.01	0.93 ± 0.01
800	1.81 ± 0.03	1.86 ± 0.04	0.98 ± 0.02	0.97 ± 0.02
1000	1.63 ± 0.03	1.63 ± 0.04	0.99 ± 0.02	0.96 ± 0.02

**Table 6**. Efficiencies for the pair produced B and $X_{5/3}$ going to dileptons and trileptons containing two opposite-sign leptons. Efficiencies contain the cuts losses, b-tagging performance and BR's of W boson.

	dilept eff.		trilept eff.	
M[GeV]	for B [%]	for $X_{5/3}$ [%]	for B [%]	for $X_{5/3}$ [%]
400	0.50 ± 0.01	0.49 ± 0.01	0.12 ± 0.01	0.12 ± 0.01
600	0.68 ± 0.01	0.69 ± 0.01	0.22 ± 0.01	0.22 ± 0.01
800	0.65 ± 0.01	0.74 ± 0.01	0.26 ± 0.01	0.25 ± 0.01
1000	0.63 ± 0.01	0.70 ± 0.01	0.28 ± 0.01	0.27 ± 0.01

Table 7. Efficiencies for the single produced B and $X_{5/3}$ going to dileptons and trileptons containing two opposite-sign leptons. Efficiencies contain the cuts losses, b-tagging performance and BR's of W boson.

a totally composite top right and top partners in a four-plet. For this we again employ simplified models with only two top partners but this time we use exact couplings corresponding to typical points in the parameter space. Therefore apart from the right-handed coupling which is still dominant there is a small admixture of the left-handed one. We present the results for $X_{5/3}$ and B masses in a range $400 - 1000\,GeV$ in tables 6 and 7 for pair and single production respectively.

Now, by using the obtained efficiencies together with the method elaborated above for computing the cross sections, one can compute the number of signal events in dileptons and trileptons and check if it falls into the region allowed by figure 12.

In figure 8 we show the excluded region in the $(\xi, M_{X^{5/3}})$ plane, where $\xi = (\frac{v}{f})^2$, depending on whether the single production is suppressed ($c_1 = 0.3$) or enhanced ($c_1 = 3$) and whether also B contributes to the signal ($M_B \gtrsim M_{X_{5/3}}$, $y = 0.3$) or not ($M_B \gg M_{X_{5/3}}$, $y = 3$). Figure 9 shows the exclusion in terms of $M_{X_{5/3}}$ and c_1. Since, as was discussed in section 3.2, the leading contribution to single production couplings is the same for
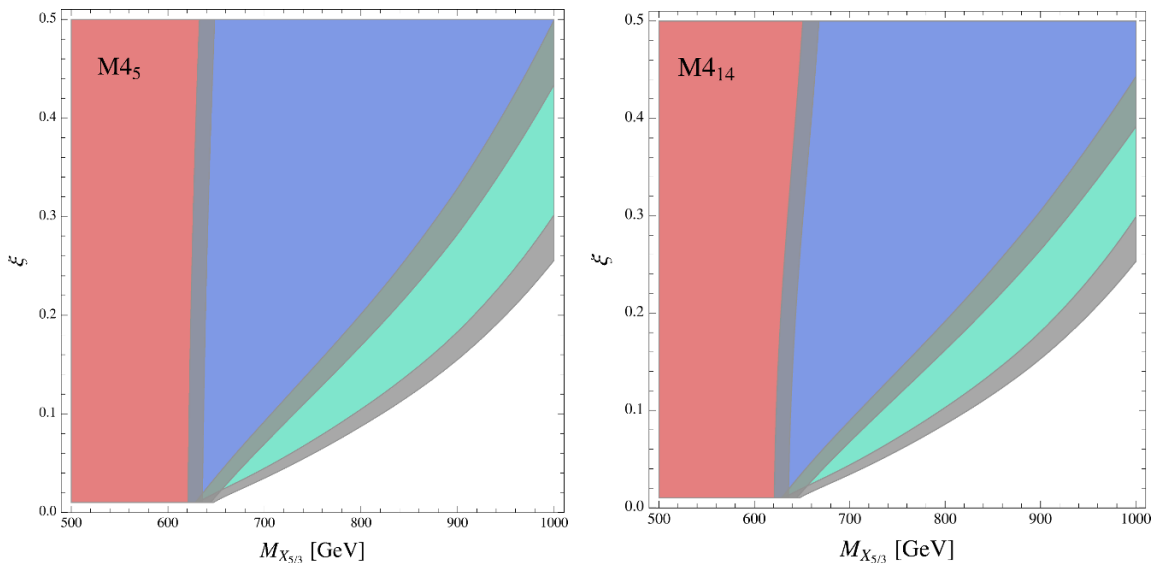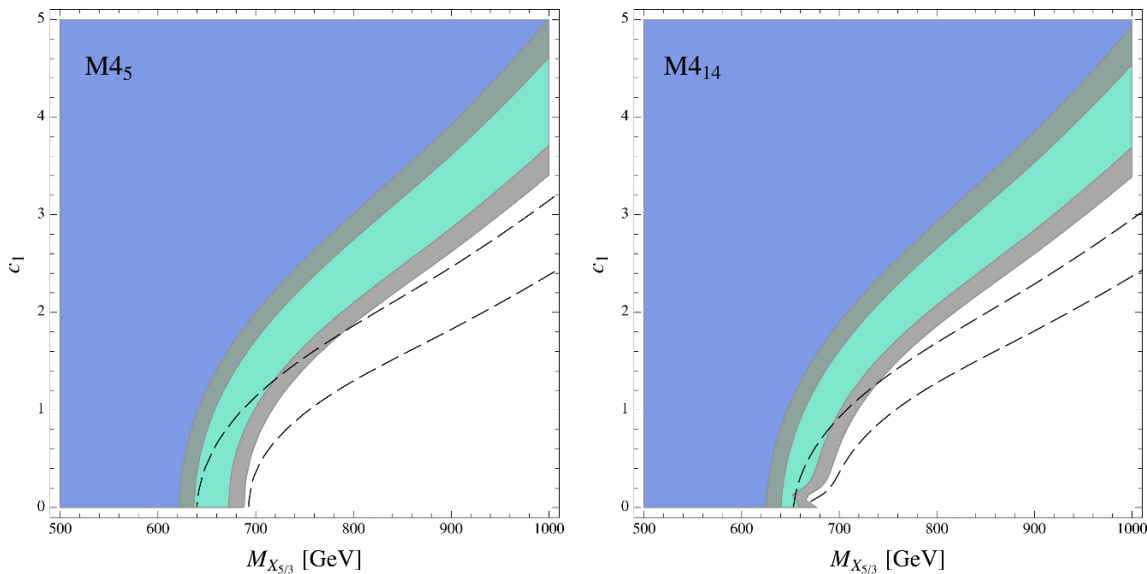
Figure 8. Excluded (95%CL) regions in the $(M_{X_{5/3}}, \xi)$ plane for the models $\mathbf{M4}_5$ and $\mathbf{M4}_{14}$, using the search for $b' \to W t$. In red: $c_1 = 0.3$ and $y = 3$ ($M_B \gg M_{X_{5/3}}$), in blue: $c_1 = 3$ and $y = 3$ ($M_B \gg M_{X_{5/3}}$), in green: $c_1 = 3$ and $y = 0.3$ ($M_B \gtrsim M_{X_{5/3}}$ for $\xi \gtrsim 0.1$, $M_B \gg M_{X_{5/3}}$ for $\xi \ll 0.1$). Gray regions correspond to a variation of the dileptons and trileptons signal of approximately 10% and 30% respectively (see text for details).

models $\mathbf{M4}_5$ and $\mathbf{M4}_{14}$, the excluded regions are also similar for both models. A difference shows up when $c_1 \ll 1$ and the $h\bar{B}b$ vertex of model $\mathbf{M4}_{14}$ becomes important thus decreasing $\mathrm{BR}(B \to Wt)$ and also when $\frac{y}{g_\psi}\epsilon = \mathcal{O}(1)$ and higher order effects modify the single production couplings. The excluded regions are almost symmetric with respect to $c_1 \to -c_1$, which can be understood as follows. When only $X_{5/3}$ production matters, the single production rate is proportional to $|c_1|^2$ at lowest order in ϵ. Higher order terms only matter in the region of small $|c_1|$ where the single production rate is anyway negligible and the bound is driven by pair production which is insensitive to c_1. When B production matters, that is because $m_B - m_{X_{5/3}} \ll m_{X_{5/3}}$, corresponding to $y \ll g_\psi$. From eq. (3.8) it is then evident that in this regime the couplings of both particles are approximately $\propto c_1$, so that the signal yield is again symmetric under $c_1 \to -c_1$. The gray regions on the plots correspond to an estimate of the mentioned above error in the determination of the efficiencies.

4.2 Search for $t' \to Z t$

The search in ref. [51] is designed to detect an up-type 4th generation quark t' pair-produced by QCD and decaying to Zt. The search is performed in the trilepton channel, with two same-flavor and opposite-charge leptons with an invariant mass around the Z pole. Moreover, at least two jets are required. Apart from the usual hardness and isolation cuts for jets and leptons an important event selection is performed with the variable R_T, defined as the scalar sum of the reconstructed momenta *without* including the two hardest leptons and the two hardest jets. R_T is required to be above $80\,\mathrm{GeV}$. With $1.14\ fb^{-1}$ of $7\,\mathrm{TeV}$ data the bound on the t' is of $475\,\mathrm{GeV}$.

Figure 9. Excluded (95%CL) regions in the $(M_{X_{5/3}}, c_1)$ plane for $\xi = 0.2$ for the models $\mathbf{M4}_5$ and $\mathbf{M4}_{14}$, using the search for $b' \to W t$. In blue: $y = 3$ ($M_B \gg M_{X_{5/3}}$), in green: $y = 0.3$ ($M_B \gtrsim M_{X_{5/3}}$). Black dashed lines correspond to the exclusions with $\xi = 0.4$. Gray regions correspond to a variation of the dileptons and trileptons signal of approximately 10% and 30% respectively (see text for details).

All the top partners of charge $2/3$ can contribute to this final state,[15] these are $X_{2/3}$ and T in models $\mathbf{M4}_5$ and $\mathbf{M4}_{14}$ and $\widetilde{T}$ in models $\mathbf{M1}_5$ and $\mathbf{M1}_{14}$. Remember however that the masses and the couplings of $X_{2/3}$ and of T are closely tight to those of, respectively, $X_{5/3}$ and B. Namely, the masses are similar (or equal) and the couplings at the leading order (see eq. (3.8)) differ by a factor of $\sqrt{2}$. Therefore the search of charge $2/3$ states will constrain the same combinations of the fundamental parameters of the model. But the bound on the charge $2/3$ partners which can be obtained using ref. [51] is by far less stringent than the one from the $b' \to W t$ search [50] described above. Given approximately 5 times less of analyzed data the limit on the production cross section of ref. [51] is significantly looser than the one of the ref. [50]. Moreover in our model the production yield of the charge-$2/3$ states is typically lower than the one of the $X_{5/3}$ and of the B. This is because of the branching ratio suppression to reach the tZ final state and because the single production rate is smaller (see section 3.3). Therefore we can safely ignore ref. [51] when constraining models $\mathbf{M4}_5$ and $\mathbf{M4}_{14}$. And moreover, for the reasons described above, we expect that, even by updating the search of ref. [51] to the same integrated luminosity of ref. [50], it would not become more important.

Hence in the following we will only use the search for $t' \to Z t$ to constrain the parameters of models $\mathbf{M1}_5$ and $\mathbf{M1}_{14}$. As in the previous section, we will obtain semi-analytical formulae for the signal yield by computing the efficiencies at each mass point and multiplying with the production cross section computed in section 3.1. Differently from the

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[15]Actually because of the quite loose cuts on the invariant mass of leptonic Z used in this search also the $X^{5/3}$ and the B could contribute, however this effect is subdominant.

previous case, the search is performed in a single channel. Therefore we will not need any statistical analysis, we will just compare the computed signal yield with the 95% CL limit obtained in ref. [51] which corresponds to 9.6 signal events.

Efficiencies

The efficiencies are computed with a MadGraph model which incorporates $\widetilde{T}$ and its couplings to Zt, ht and Wb. These are responsible for the two single production modes and for the decay. The $\widetilde{T}$ couples only to left-handed quarks, therefore in this case we will employ left-handed couplings to compute the efficiencies. Our results can thus be directly compared with the efficiencies reported in ref. [51] because the coupling is left-handed also in the case of a 4th family quark.

The $\widetilde{T}$ can contribute to the signal both in the pair and in the single production mode, provided that at least one $\widetilde{T}$ decays to Zt paying a branching fraction of around $1/4$ (see section 3.3). In the case of pair production all the decay modes of the second produced $\widetilde{T}$ (Zt, Wb or ht) are potentially relevant. We have computed separately the efficiencies in all three cases. The methodology of the analysis, and in particular the treatment of the experimental efficiencies, closely follows the one of the previous section. The results are shown in table 8, our efficiencies contain the cut losses and the W, Z, h branching fractions to the required final state. The efficiencies listed in the first column of the table can be directly compared with the ones of ref. [51], we have checked that the discrepancy is around 25% which corresponds to approximately 1.5σ of the signal uncertainty obtained in the ref. [51].

We see in table 8 that the efficiency for the single production with the b is extremely low, below 1 ‰. This is because the single production signal (see figure 3) is characterized by three leptons plus one hard (b) jet from the top decay, plus one forward jet from the virtual W emission and a $\bar{b}$ from the gluon splitting. But the gluon splitting is enhanced in the collinear region, therefore the b-jet emitted from the gluon is also preferentially forward and with low p_T. In order for the event to pass the selection cut, that requires at least two jets with $p_T > 25\,\mathrm{GeV}$ and $|\eta| < 2.4$, at least one of the two preferentially forward jets must be central and hard enough, implying a significant reduction of the cross-section. However this is not yet the dominant effect, the main reduction of the signal is due to the cut $R_T > 80\,\mathrm{GeV}$ discussed before. Indeed R_T is computed without including the two hardest leptons and the two hardest jets, which in our case means, since we have only 3 leptons and typically only 2 jets, that the momentum of the softest lepton must be above $80\,\mathrm{GeV}$. Therefore in the end the signal is completely killed. The situation is better for the single production with the t since one typically has more particles produced in this case and therefore the efficiencies are comparable with the ones of pair production.

The situation is better for the single production with the t, the efficiencies are comparable with the ones of pair production (see table 8). However, we have seen in section 3.3 (see figure 7) that the rate of pair production is typically larger than the one of single production with the top, in the relevant mass range. Since the efficiencies are comparable we do not expect a sizable contribution from this process. The signal is totally dominated by the pair production and the $\mathrm{BR}(\widetilde{T} \to Zt)$ is fixed to be about $1/4$, as discussed in

	pair prod. eff. [%]			single prod. eff. [%]	
M [GeV]	$T\bar{T} \to Zt\,Z\bar{t}$	$T\bar{T} \to Zt\,W\bar{b}$	$T\bar{T} \to Zt\,h\bar{t}$	$T\,\bar{t}\,j$	$T\,\bar{b}\,j$
300	1.78	1.22	1.51	1.13	0.03
350	1.93	1.47	1.64	1.17	0.03
450	2.21	1.81	1.81	1.25	0.05
550	2.34	1.93	1.95	1.30	0.06
650	2.40	2.12	1.96	1.35	0.08

Table 8. Cuts efficiencies for the charge 2/3 top partners going to trileptons for the case of pair production and different decay channels, and a single production for the cases of Z-t fusion(4th column) and W-b fusion(5th column). Efficiencies contain the cuts losses and BR's of W, Z and the SM Higgs boson.

section 3.3. Therefore the bounds one can infer are mainly on $m_{\widetilde{T}}$, but a mild dependence on the other parameters (ξ and y) is still residual in the BR. The resulting bound is about $m_{\widetilde{T}} \gtrsim 320\,\mathrm{GeV}$ in both models $\mathbf{M1}_5, \mathbf{M1}_{14}$, and it is maximized at large ξ and small y $m_{\widetilde{T}} \gtrsim 350\,\mathrm{GeV}$ in model $\mathbf{M1}_{14}$. These bounds are not competitive with those coming from the $t' \to W\,b$ search, as we are going to discuss next.

4.3   Search for $t' \to W\,b$

The last experimental study that we are going to consider is the search for a 4th generation t' quark decaying to Wb [52]. The search is performed in the channel of two opposite sign leptons (away from the Z pole) with two tagged bottom quarks. A very important selection cut, which is needed to suppress the background from the top quark production, is that the invariant mass of all the lepton and b-jet pairs, M_{lb}, is above 170 GeV. This forbids that the lepton and the b originate from the decay of a top quark. Using data from $5\,fb^{-1}$ of integrated luminosity, a lower bound of $557\,\mathrm{GeV}$ was set on the t' mass [52].

In our models, only $\widetilde{T}$ can decay to Wb with a sizable branching fraction. We will therefore use ref. [52] to put constraints on models $\mathbf{M1}_5$ and $\mathbf{M1}_{14}$.[16] The single production mode with the b is definitely not relevant in this case because it only leads to one lepton. The one with the t is also irrelevant because the second lepton would come from the decay of the top quark and it would not satisfy the cut on M_{lb}. We are therefore left with pair production. Moreover, because of the $M_{bj} > 170\,\mathrm{GeV}$ cut, and as was explicitly checked in ref. [55], pair production contributes to the signal only if both $\widetilde{T}$'s decay to Wb. We are then left with the same channel, $\widetilde{T}\overline{\widetilde{T}} \to WbWb$, considered in ref. [52]. The chirality of the coupling responsible for the decay is also the same as in the 4th family case. Therefore the efficiencies can be extracted directly from ref. [52] without any need for additional simulations. Given the efficiency and taking into account that the branching fraction of

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[16]Also pair produced B and $X_{5/3}$ decaying to Wt contributes to the final states considered in ref. [52]. However the resulting bound on these states is lower than the one obtained using ref. [50]. In addition the signature used in ref. [52] is insensitive to single production. Thus we do not expect any improvement of the bounds on the models $\mathbf{M4}_5$ and $\mathbf{M4}_{14}$ from this search.
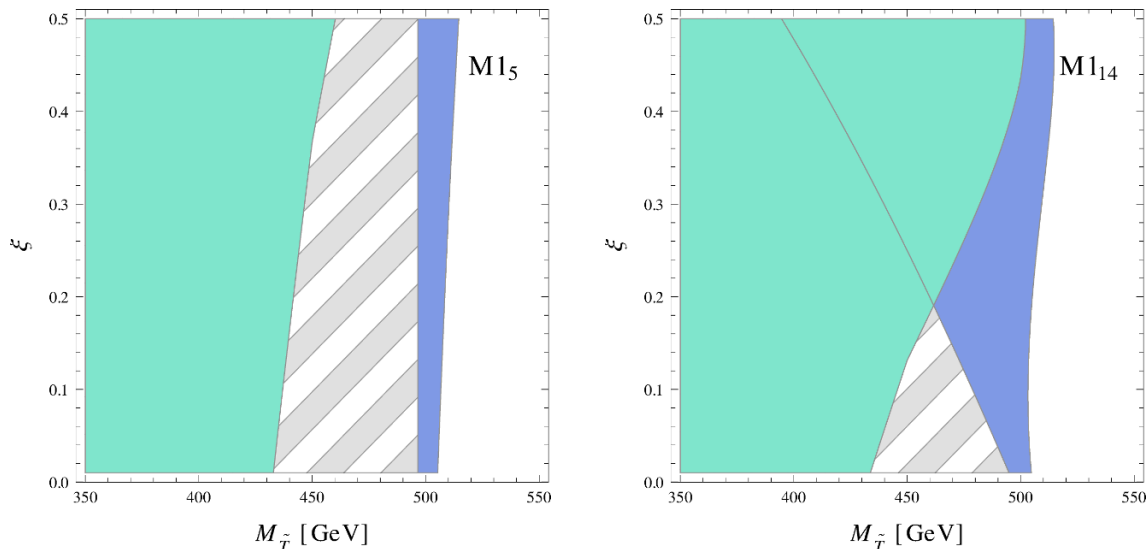
Figure 10. Excluded (95%CL) regions in the $(M_{\widetilde{T}}, \xi)$ plane, using the search $t' \to Wb$, for the models $\mathbf{M1}_5$ and $\mathbf{M1}_{14}$ for $y = 0.5$ (green), $y = 2$ (blue) (corresponding approximately to $c_2 \simeq 2$ (green), $c_2 \simeq 0.5$ (blue)). In the gray dashed region there are no solutions for $M_{\widetilde{T}}(y, \xi)$ when $y = 2$.

the $\widetilde{T}$ to Wb, we can easily compute the signal yield and compare it with the bound obtained in [52].

Plots and results

We show the excluded regions of the parameter space in terms of ξ and $M_{\widetilde{T}}$ on the figure 10. The exclusion is stronger for larger y (and smaller c_2) due to a larger $BR(\widetilde{T} \to Wb)$ in this case. As was already discussed in the section 3.2 the gauge interactions of the model $\mathbf{M1}_{14}$ are similar to the ones of the model $\mathbf{M1}_5$ and therefore the excluded regions are also similar. The difference is sizable in the region close to $\xi = 0.5$ where in the model $\mathbf{M1}_{14}$ interactions with a Higgs boson vanish according to eq. (B.7) and therefore the BR of the competitive decay to Wb increases. The regions without solutions for $\widetilde{T}(y, \xi)$ when y is large correspond to those defined by the eq. (2.28).

Due to a larger amount of data analyzed and a higher BR of the $\widetilde{T} \to Wb$ decay mode the search of ref. [52] gives a better constraint on the parameters of our models than the previously considered search $\widetilde{T} \to Zt$ [51]. However one may expect that with increased amount of analyzed data the search for $\widetilde{T} \to Zt$ can become competitive due to its sensitivity to single production.

4.4 Summary of exclusions

The results of the searches described above can be conveniently summarized by scanning over the values of the model parameters and selecting the most and the least stringent bounds on the top-partners' masses. The highest excluded masses of $X_{5/3}$ and $X_{2/3}$ correspond to the lowest value of y and highest c_1 and ξ, and the opposite for the lowest
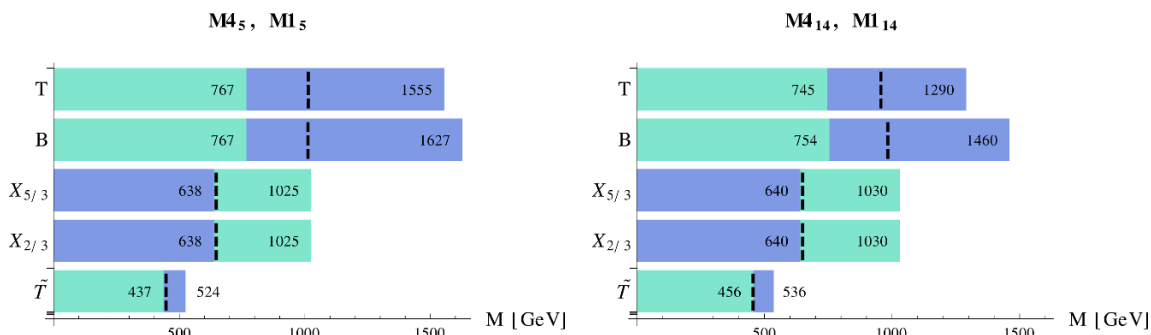
Figure 11. Maxmal and minimal bounds on the masses of top partners for $y \in [0.3, 3]$, $c_1 \in [0.3, 3]$ and $\xi \in [0.1, 0.3]$ for the models $\mathbf{M4}_5$, $\mathbf{M1}_5$ (left pannel) and $\mathbf{M4}_{14}$, $\mathbf{M1}_{14}$ (right pannel). Blue and green bars correspond respectively to high and low values of y. Black dashed lines correspond to the exclusions for the reference values $\xi = 0.1$, $c_1 = 1$, $y = 1$.

exclusion. For T and B the highest exclusion corresponds to the highest y, c_1 and ξ and the opposite for the lowest exclusion. Maximal $\widetilde{T}$ mass exclusion is reached when y and ξ are maximal and the minimal exclusion is obtained for minimal y and ξ. In figure 11, we show our results for the maximal and minimal exclusions obtained by varying the parameters in the ranges: $y \in [0.3, 3]$, $c_1 \in [0.3, 3]$ and $\xi \in [0.1, 0.3]$.

5 Conclusions

In this paper we described an approach to systematically construct the low-energy effective lagrangian for the lighest colored fermion multiplet related to the UV completion of the top quark sector: the top partner. Our construction is based on robust assumptions, as concerns symmetries, and on plausible assumptions, as concerns the dynamics. Our basic dynamical assumption, following ref. [4], is that the electroweak symmetry breaking sector, or at least the fermionic sector, is broadly decribed by a coupling g_* and a mass scale m_*. This assumption implies a well definite power counting rule. In particular the derivative expansion is controlled by inverse powers of m_*. In the technical limit where the top partner multiplet Ψ, is parametrically much lighter than the rest of the spectrum ($M_\Psi \ll m_*$), our power counting provides a weakly coupled effective lagrangian description of the phenomenology of Ψ. The basic idea is that, in this case, the effects of the bulk of the unknown spectrum at the scale m_* can be systematically described by an expansion in powers of M_Ψ/m_*. The lagrangian obtained in this limit defines our simplified description of the top parters. One should however keep in mind that the most likely physical situation is one where $m_* - M_\Psi \sim M_\Psi$, where an effective lagrangian is formally inappropriate. In practice, however, we expect it to be more than adequate for a first semi-quantitative description of the phenomenology and certainly to assess experimental constraints. The comparison with explicit constructions supports this expectation.

As concerns the symmetries of the strong sector, we considered the minimal composite Higgs based on the SO(5)/SO(4) coset. Furthermore we focussed on the simplest possibility where the right-handed top quark t_R is itself a composite fermion. The leading source of

breaking of SO(5) is thus identified with top quark Yukawa coupling y_t. In our construction, we have fully exploited the selection rules obtained by treating y_t as a small spurion with definite transformation properties. For instance the structure of the mass spectrum and the couplings are greatly constrained by symmetry and selection rules. In particular the pNGB nature of the Higgs doublet implies the couplings originating from the strong sector are purely derivative: at high energy, or for heavy on-shell fermions, these couplings are effectively quite sizeable and yet they do not affect the spectrum even accounting for $\langle H \rangle \neq 0$. If the Higgs were not treated as a pNGB a large trilinear would be associated with a large Yukawa coupling and the spectrum would necessarily be affected when $\langle H \rangle \neq 0$.

Depending on the quantum numbers of the top partner multiplet Ψ and of the composite operator $\mathcal{O}$ that seeds the top Yukawa in the microscopic theory, one can then consider a variety of models. We focussed on the four possibilities shown in table 1, which could be considered the simplest ones. Our method can however be directly applied to perhaps more exotic possibilities. For instance one exotic, but not implausible, case would be $\mathcal{O} = \mathbf{14_{2/3}}$ with Ψ in the symmetric traceless tensor of SO(4), that is $\Psi = \mathbf{9_{2/3}}$. This case involves a top partner with electric charge 8/3, performing a spectacular chain decay to $3W^+ + b$.

Our effective lagrangian depends on a manageable number of parameters. Once the top mass is fixed, beside the Goldstone decay constant f and the partner mass M_Ψ, there remain, depending on the model, only one or two additional parameters. These parameters, $c_{1,2}$, control the size of the trilinear couplings between Ψ, third family fermions, and vector bosons or Higgs. They thus control the decay and the single production of top partners. Moreover, naive power counting suggests a preferred $O(1)$ range for these parameters. This fact, coupled with the constraints due to symmetry, robustly implies a definite structure for the interactions vertices in each model. For instance, for the case where Ψ spans an SO(4) quadruplet, the trilinear coupling to the Higgs doublet involves mostly a t_R and is expected to be of the order of a strong sector coupling $g_\Psi = M_\Psi/f$. Moreover it grows with M_Ψ making simple production even more important in the range of heavy Ψ. In the case of a singlet Ψ, the trilinear is of order y_t and involves the left handed doublet $(t, b)_L$. These details, including the chirality of the top, affect the collider phenomenology of the models and, consequently, the constraints from searches.

Not only have we a few lagrangian parameters, but also they mainly affect phenomenology via their contribution to the trilinear couplings. Using this property we devised a semi-analytical way to efficiently simulate the contribution of single production to the signal. For any given mass M_Ψ, we numerically simulated single production once for all, assigning trilinear coupling equal to unity. The physical cross section was then obtained by folding this numerical result with the analytical dependence of the physical trilinear coupling on the model parameters. Thus, once the efficiencies associated with a given experimental search are known, the constraint in parameter space can be obtained analytically. We implemented the calculation of the cross-sections in a *Mathematica* notebook which is available on request.

We applied our results to the presently available LHC searches. We focussed on the search for 4th family fermions, that have signatures similar to those of top partners, and recast them to constrain our models. The main results can be read from figure 9 and

figure 10. The former figure shows that, in the relevant region $c_1 = O(1)$, single production has a mild but non-negligible impact on the bounds.

In the course of our analysis, it became evident that there exists significant space for improvement in the search strategy if one wants to best constrain this class of models. The searches we used were tailored to pair production of heavy quarks, while single production of top partners has different features. First of all, in single production there is only one hard decaying object, with the t or b produced in association beeing often less hard (much more so in the case of a b): the cuts performed in present searches tends to penalize single production. Secondly, single production is always associated with a very forward jet, originating from the collinear splitting of a typically valence quark into a longitudinally polarized vector boson. The resulting forward jet has exactly the same features of the tag jets of WW scattering. There is a good chance the use of the same tag in the searches for singly produced top partners would significantly extend the sensitivity. We also realized that the single production with the b is typically very large (see figure 7) in the case of a singlet top partner $\widetilde{T}$, tagging this production mechanism would increase significantly the LHC sensitivity to this kind of particles. Ideally the best channel of detection would be the resonant Wb production from the $\widetilde{T}$ decay, accompanied by one forward jet from the longitudinal vector boson emission. The second b quark which is present in the reaction, which comes from the gluon splitting as in figure 3, is typically quite soft both in $p_\perp$ and in energy. Thus it is probably strongly affected by QCD initial state radiation and difficult to detect. Building upon these considerations, it would be worth to undertake a thorough experimental analysis, including the effect of radiation and detector simulation, suitably designed for the search of singly produced top-partners.

In the test of weak scale naturalness, the search for all possible fermionic top partners represents the other half of the sky. In this paper we have introduced a first systematic description of top partner phenomenology. The simplicity of the result should hopefully serve as a basis for future systematic experimental studies. As seen from our theorist's analysis, the present searches have already advanced well into the region suggested by naturalness. But there is no doubt somebody out there can do better.

Acknowledgments

A Explicit CCWZ construction for SO(5)/SO(4)

Generators and Goldstone matrix

The generators of SO(5) in the fundamental representation are conveniently chosen to be

$$(T^\alpha_{L,R})_{IJ} = -\frac{i}{2}\left[\frac{1}{2}\varepsilon^{\alpha\beta\gamma}\left(\delta^\beta_I\delta^\gamma_J - \delta^\beta_J\delta^\gamma_I\right) \pm \left(\delta^\alpha_I\delta^4_J - \delta^\alpha_J\delta^4_I\right)\right], \tag{A.1}$$

$$T^i_{IJ} = -\frac{i}{\sqrt{2}}\left(\delta^i_I\delta^5_J - \delta^i_J\delta^5_I\right), \tag{A.2}$$

where $T^\alpha_{L,R}$ ($\alpha = 1,2,3$) are the $SO(4) \simeq SU(2)_L \times SU(2)_R$ unbroken generators, while T^i ($i = 1,\ldots,4$) are the broken ones and parametrize the coset SO(5)/SO(4). An equivalent notation for unbroken generators which we will use is T^a with $a = 1,\ldots,6$. The indices IJ take the values $1,\ldots,5$. The normalization of the T^A's is chosen as $\text{Tr}[T^A, T^B] = \delta^{AB}$.

The T^α_L and T^α_R generators span respectively the $SU(2)_L$ and $SU(2)_R$ subgroups, and obey the standard commutation relations

$$\left[T^\alpha_{L,R}, T^\beta_{L,R}\right] = i\varepsilon^{\alpha\beta\gamma}\,T^\gamma_{L,R}. \tag{A.3}$$

The T_L's are therefore identified as the generators of the SM $SU(2)_L$. Notice that in our parametrization the unbroken T^a's are block-diagonal

$$T^a = \begin{pmatrix} t^a & 0 \\ 0 & 0 \end{pmatrix}, \tag{A.4}$$

and the generators obey the following commutation relation

$$\left[T^a, T^i\right] = (t^a)_{ji}\,T^j. \tag{A.5}$$

With these generators, the parametrization of the Goldstone boson matrix is explicitly given by

$$U = \text{U}(\Pi) = \exp\left[i\frac{\sqrt{2}}{f}\Pi_i T^i\right] = \begin{pmatrix} \mathbf{1}_{4\times 4} - \frac{\vec{\Pi}\vec{\Pi}^T}{\Pi^2}\left(1 - \cos\frac{\Pi}{f}\right) & \frac{\vec{\Pi}}{\Pi}\sin\frac{\Pi}{f} \\ -\frac{\vec{\Pi}^T}{\Pi}\sin\frac{\Pi}{f} & \cos\frac{\Pi}{f} \end{pmatrix} \tag{A.6}$$

where $\Pi^2 \equiv \vec{\Pi}^t\vec{\Pi}$. Under $g \in SO(5)$, the Goldstone matrix transforms as

$$\text{U}(\Pi) \;\to\; \text{U}(\Pi^{(g)}) = g \cdot \text{U}(\Pi) \cdot h^t(\Pi; g), \tag{A.7}$$

where $h(\Pi; g)$ is block-diagonal in our basis

$$h = \begin{pmatrix} h_4 & 0 \\ 0 & 1 \end{pmatrix}, \tag{A.8}$$

with $h_4 \in SO(4)$. Under the unbroken SO(4) the Π's transform *linearly*, using eq. (A.5) we get $\Pi^i \to (h_4)^i{}_j\Pi^j$. Given our embedding of the SM group, the Π four-plet can be rewritten as

$$\vec{\Pi} = \begin{pmatrix} \Pi_1 \\ \Pi_2 \\ \Pi_3 \\ \Pi_4 \end{pmatrix} = \frac{1}{\sqrt{2}}\begin{pmatrix} -i\left(h_u - h_u^\dagger\right) \\ h_u + h_u^\dagger \\ i\left(h_d - h_d^\dagger\right) \\ h_d + h_d^\dagger \end{pmatrix}, \tag{A.9}$$

where

$$H = \begin{pmatrix} h_u \\ h_d \end{pmatrix} , \tag{A.10}$$

is the standard Higgs doublet of $+1/2$ Hypercharge.

In the unitary gauge, in which

$$h_u = 0, \qquad h_d \equiv \frac{h}{\sqrt{2}} = \frac{\langle h \rangle + \rho}{\sqrt{2}} , \tag{A.11}$$

where ρ is the canonically normalized physical Higgs field, the Goldstone boson matrix of eq. (A.8) simplifies and becomes

$$U = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & \cos\frac{h}{f} & \sin\frac{h}{f} \\ 0 & 0 & 0 & -\sin\frac{h}{f} & \cos\frac{h}{f} \end{pmatrix} . \tag{A.12}$$

Given that we will have to gauge the SM subgroup of SO(5), we must consider also *local* transformations, $g = g(x)$, in the above equation. We also have to define *gauge sources* A_μ^A

$$A_\mu = A_\mu^A T^A \;\rightarrow\; A_\mu^{(g)} = g \left[A_\mu + i\partial_\mu \right] g^t , \tag{A.13}$$

some of which we will eventually make dynamical while setting the others to zero. Explicitly, the dynamical part of A_μ will be

$$A_\mu = \frac{g}{\sqrt{2}} W_\mu^+ \left(T_L^1 + iT_L^2 \right) + \frac{g}{\sqrt{2}} W_\mu^- \left(T_L^1 - iT_L^2 \right) + g \left(c_{\rm w} Z_\mu + s_{\rm w} A_\mu \right) T_L^3 + g' \left(c_{\rm w} A_\mu - s_{\rm w} Z_\mu \right) T_R^3 , \tag{A.14}$$

where $c_{\rm w}$ and $s_{\rm w}$ denote respectively the cosine and the sine of the weak mixing angle and g, g' are the SM couplings of SU(2)$_L$ and U(1)$_Y$. Notice that A_μ belongs to the unbroken SO(4) subalgebra, this will simplify the expression for the d and e symbols that we will give below.

The d and e symbols

Still treating A_μ as a general element of the SO(5) algebra, we can define the d and e symbols as follows. Start from defining

$$\bar{A}_\mu \equiv A_\mu^{(U^t)} = U^t \left[A_\mu + i\partial_\mu \right] U , \tag{A.15}$$

this transforms under SO(5) in a peculiar way

$$\bar{A}_\mu \;\rightarrow\; A_\mu^{(h \cdot U^t \cdot g^t \cdot g)} = \bar{A}_\mu^{(h)} = h \left[\bar{A}_\mu + i\partial_\mu \right] h^t \tag{A.16}$$

Since $h = h(\Pi; g)$ is an element of SO(4) as in eq. (A.8), the shift term in the above equation, $ih\partial_\mu h^t$, lives in the SO(4) subalgebra. Therefore, if we decompose $\bar{A}_\mu$ in broken and unbroken generators

$$\bar{A}_\mu \equiv - d_\mu^i T^i - e_\mu^a T^a , \tag{A.17}$$

we have that d^i_μ transforms linearly (and in the fourplet of SO(4)) while the shift is entirely taken into account by e^a_μ. We have

$$d^i_\mu \to (h_4)^i{}_j\, d^j_\mu \quad \text{and} \quad e_\mu \equiv e^a_\mu t^a \to h_4 \left[e_\mu - i\partial_\mu \right] h^t_4\,. \tag{A.18}$$

Let us now restrict, for simplicity, to the case in which A_μ belongs to the SO(4) subalgebra, as for our dynamical fields in eq. (A.14). It is not difficult to write down an explicit formula for d and e, these are given by

$$d^i_\mu = \sqrt{2}\left(\frac{1}{f} - \frac{\sin \Pi/f}{\Pi}\right) \frac{\vec{\Pi} \cdot \nabla_\mu \vec{\Pi}}{\Pi^2}\Pi^i + \sqrt{2}\frac{\sin \Pi/f}{\Pi}\nabla_\mu \Pi^i$$

$$e^a_\mu = -A^a_\mu + 4\,i\,\frac{\sin^2 (\Pi/2f)}{\Pi^2}\vec{\Pi}^t t^a \nabla_\mu \vec{\Pi} \tag{A.19}$$

where $\nabla_\mu \Pi$ is the "covariant derivative" of the Π field:

$$\nabla_\mu \Pi^i = \partial_\mu \Pi^i - iA^a_\mu (t^a)^i{}_j\, \Pi^j\,. \tag{A.20}$$

The first use we can make of the d_μ symbol is to define the SO(5)-invariant kinetic Lagrangian for the Goldstone bosons, this is given by

$$\mathcal{L}_\pi = \frac{f^2}{4}d^i_\mu d^\mu_i\,. \tag{A.21}$$

In the unitary gauge of eq. (A.11) and using eq. (A.14) for A_μ the Goldstone Lagrangian becomes

$$\mathcal{L}_\pi = \frac{1}{2}(\partial h)^2 + \frac{g^2}{4}f^2 \sin^2 \frac{h}{f}\left(|W|^2 + \frac{1}{2c_w^2}Z^2\right)\,, \tag{A.22}$$

from which we can check that the field ρ is indeed canonically normalized and read the W and Z masses $m_W = g/2f \sin \frac{\langle h\rangle}{f}$, $m_Z = m_W/c_w$. This fixes relation among $\langle v\rangle$ and the EW scale $v = 246\,\text{GeV}$

$$v = f \sin \frac{\langle h\rangle}{f}\,. \tag{A.23}$$

The e_μ symbol can instead be used to construct the CCWZ covariant derivatives, because the shift term in its transformation rule of eq. (A.18) compensates for the shift of the ordinary derivative. Consider for instance the field Ψ defined in eq. (2.5) of the main text, which transforms in the **4** of SO(4), i.e. like $\Psi \to h_4 \cdot \Psi$. The covariant derivative is

$$\nabla_\mu \Psi = \partial_\mu \Psi + i\,e^a_\mu t^a \Psi\,. \tag{A.24}$$

The CP symmetry

By looking at eq. (A) and remembering that CP acts as $H(x) \to H^*(x^{(P)})$ on the Higgs doublet we immediately obtain the action of the CP transformation on the Goldstone fields Π and on the Goldstone matrix U. It is

$$\vec{\Pi}(x) \to C_4 \cdot \vec{\Pi}(x^{(P)})\,, \qquad \text{U}(x) \to C_5 \cdot \text{U}(x^{(P)}) \cdot C_5\,, \tag{A.25}$$

where C_4 and C_5 are respectively a 4×4 and a 5×5 diagonal matrices defined as

$$C_4 = \text{diag}(-1, +1, -1, +1), \qquad C_5 = \text{diag}(-1, +1, -1, +1, +1). \qquad \text{(A.26)}$$

In the above equations the superscript "(P)" denotes the action of ordinary spatial parity. Similarly, the ordinary action of CP on the SM gauge fields in eq. (A.14) is recovered if we take

$$A_\mu \;\to\; C_5 \cdot A_\mu^{(P)} \cdot C_5 \,. \qquad \text{(A.27)}$$

From the above equations it is straightforward to derive the CP transformations of the d and e symbols defined in eq. (A.17),

$$d_\mu^i \;\to\; C_4{}^i{}_j (d_\mu^{(P)})^j \,, \qquad e_\mu \;\to\; C_4 \cdot (e_\mu^{(P)}) \cdot C_4 \,. \qquad \text{(A.28)}$$

In the fermionic sector, adopting for definiteness the Weyl basis, the CP transformation of the q_L and of the t_R are the usual ones

$$\chi(x) \;\to\; \chi^{(CP)} = i\gamma^0 \gamma^2 \psi^*(x^{(P)}) \,, \qquad \text{(A.29)}$$

for $\chi = \{t_L, b_L, t_R\}$. For the top partners, in the case in which they transform in the fourplet of SO(4) as in eq. (2.5), it is natural to define CP as

$$\Psi_i \;\to\; C_4{}_i{}^j \Psi_j^{(CP)} \,, \qquad \text{(A.30)}$$

while for the case of the singlet we simply have $\Psi \;\to\; \Psi^{(CP)}$. Notice that with this definition the charge eigenstate fields $\{T, B, X_{2/3}, X_{5/3}\}$ defined in eq. (2.5) have "ordinary" CP transformation as in eq. (A.29);

B Fermion couplings

In this appendix we report the explicit form of the fermion couplings to gauge bosons and to the Higgs, in the unitary gauge defined by eq. (A.11), that arise in our four models $\mathbf{M4}_5$, $\mathbf{M4}_{14}$, $\mathbf{M1}_5$ and $\mathbf{M1}_{14}$, defined respectively in eqs. (2.7), (2.11) and (2.12). All the couplings are given *before* the rotations that diagonalize the mass-matrices.

The first two terms, which are relevant for the models $\mathbf{M4}_5$ and $\mathbf{M4}_{14}$, are

$$
\begin{aligned}
i\,\overline{\Psi}_R^i \slashed{d}_i t_R = \;\; & \frac{g}{\sqrt{2}} \sin\frac{h}{f} (\overline{X}_{5/3})_R \slashed{W}^+ t_R - \frac{g}{\sqrt{2}} \sin\frac{h}{f} \overline{B}_R \slashed{W}^- t_R - \frac{g}{2c_w} \sin\frac{h}{f} \overline{T}_R \slashed{Z} t_R \\
& - \frac{g}{2c_w} \sin\frac{h}{f} (\overline{X}_{2/3})_R \slashed{Z} t_R + i\left[(\overline{X}_{2/3})_R - \overline{T}_R \right] \frac{\slashed{\partial}\rho}{f} t_R \,,
\end{aligned} \qquad \text{(B.1)}
$$

and the term with the e_μ symbol which we combine, for convenience, with the one from the covariant derivative in eq. (2.10)

$$
\begin{aligned}
\overline{\Psi}\left(\frac{2}{3}g'\slashed{B} - \slashed{e}\right)\Psi =\ & \frac{g}{c_w}\left(-\frac{1}{2} + \frac{1}{3}s_w^2\right)\overline{B}\slashed{Z}B + \frac{g}{c_w}\left(\frac{1}{2} - \frac{5}{3}s_w^2\right)\overline{X}_{5/3}\slashed{Z}X_{5/3} \\
& + \frac{g}{c_w}\left(\frac{1}{2}\cos\frac{h}{f} - \frac{2}{3}s_w^2\right)\overline{T}\slashed{Z}T + \frac{g}{c_w}\left(-\frac{1}{2}\cos\frac{h}{f} - \frac{2}{3}s_w^2\right)\overline{X}_{2/3}\slashed{Z}X_{2/3} \\
& + \left\{\frac{g}{\sqrt{2}}\overline{B}\slashed{W}^-\left[\cos^2\frac{h}{2f}T + \sin^2\frac{h}{2f}X_{2/3}\right]\right. \\
& + \frac{g}{\sqrt{2}}\overline{X}_{5/3}\slashed{W}^+\left[\sin^2\frac{h}{2f}T + \cos^2\frac{h}{2f}X_{2/3}\right] + \left. h.c.\right\} \\
& + \text{``photon couplings''}.
\end{aligned}
\tag{B.2}
$$

The couplings to the photon are not reported explicitly in the above equation because they are simply the standard ones, being completely fixed by the $U(1)_{\text{em}}$ residual gauge symmetry.

In addition to the ones in eq. (B.2), non-derivative couplings with the Higgs field emerge in model $\mathbf{M4}_5$ from the terms

$$
\begin{aligned}
yf\,(\overline{Q}_L^{\mathbf{5}})^I U_{I\,i}\Psi_R^i &= yf\,\bar{b}_L B_R + yf\,\bar{t}_L\left[\cos^2\frac{h}{2f}T_R + \sin^2\frac{h}{2f}(X_{2/3})_R\right], \\
yc_2 f\,(\overline{Q}_L^{\mathbf{5}})^I U_{I\,5}t_R &= -\frac{yc_2 f}{\sqrt{2}}\sin\frac{h}{f}\bar{t}_L t_R,
\end{aligned}
\tag{B.3}
$$

while in model $\mathbf{M4}_{14}$ we have

$$
\begin{aligned}
yf\,(\overline{Q}_L^{\mathbf{14}})^{I\,J} U_{I\,i} U_{J\,5}\,\Psi_R^i &= yf\,\cos\frac{h}{f}\bar{b}_L B_R \\
& + \frac{yf}{2}\bar{t}_L\left[\left(\cos\frac{h}{f} + \cos\frac{2h}{f}\right)T_R + \left(\cos\frac{h}{f} - \cos\frac{2h}{f}\right)(X_{2/3})_R,\right] \\
\frac{yc_2 f}{2}(\overline{Q}_L^{\mathbf{14}})^{I\,J} U_{I\,5} U_{J\,5}\,t_R &= -\frac{yc_2 f}{2\sqrt{2}}\sin\frac{2h}{f}\bar{t}_L t_R.
\end{aligned}
\tag{B.4}
$$

For the models with the singlet, $\mathbf{M1}_5$ and $\mathbf{M1}_{14}$, the only gauge-fermion interactions come from the covariant derivative

$$
\frac{2}{3}g'\overline{\Psi}\slashed{B}\Psi = -\frac{2}{3}\frac{g}{c_w}s_w^2\overline{\widetilde{T}}\slashed{Z}\widetilde{T} + \frac{2}{3}e\,\overline{\widetilde{T}}\slashed{A}\widetilde{T}.
\tag{B.5}
$$

The couplings with the Higgs come instead from

$$
\begin{aligned}
yf\,(\overline{Q}_L^{\mathbf{5}})^I U_{I\,5}\Psi_R &= -\frac{yf}{\sqrt{2}}\sin\frac{h}{f}\bar{t}_L\widetilde{T}_R, \\
yc_2 f\,(\overline{Q}_L^{\mathbf{5}})^I U_{I\,5}\,t_R &= -\frac{yc_2 f}{\sqrt{2}}\sin\frac{h}{f}\bar{t}_L t_R,
\end{aligned}
\tag{B.6}
$$

for model $\mathbf{M1}_5$ and from

$$
\begin{aligned}
\frac{y}{2}f\,(\overline{Q}_L^{\mathbf{14}})^{I\,j} U_{I\,5} U_{J\,5}\Psi_R &= -\frac{yf}{2\sqrt{2}}\sin\frac{2h}{f}\bar{t}_L\widetilde{T}_R, \\
\frac{yc_2}{2}f\,(\overline{Q}_L^{\mathbf{14}})^{I\,j} U_{I\,5} U_{J\,5}\,t_R &= -\frac{yc_2 f}{2\sqrt{2}}\sin\frac{2h}{f}\bar{t}_L t_R.
\end{aligned}
\tag{B.7}
$$

for model $\mathbf{M4}_{14}$.

C   Statistical tools

In the analysis performed in the ref. [50] the CL_s method is used to obtain the exclusion confidence intervals for the mass of the b' quark. However this exclusion is made in terms of the pair production cross section assuming some fixed ratio between the yield in dileptons and trileptons channels. In our case this ratio depends on the relative strength of the single and pair production and can significantly deviate from the one used in the ref. [50]. Thus we want to re-do part of the experimental analysis in order to extract a more model-independent exclusion in terms of the number of di- and trileptons separately. Though we are not restricted to using the CL_s only, we think that this method is well suited for constraining the parameter space of our model.

To use the CL_s we first construct a test statistics q as a log-ratio of probability density for the signal+background hypothesis to the background hypothesis:

$$q = -2 \log \prod_{i=2l,3l} \frac{P(n_i|s_i + b_i)}{P(n_i|b_i)} \tag{C.1}$$

where n_i - number of observed in the pseudo-experiment di- and trilepton events, s_i and b_i - number of the signal and background events respectively. The distribution P for a small number of events can be taken as a Poissonian modified due to the presence of the uncertainties. The largest uncertainty in the experimental analysis comes from the background estimation and can be accounted for by taking a marginal probability density defined as

$$P(n_i|s_i + b_i) = \int \mathcal{P}(n_i|s_i + \nu_i b_i) \, ln\mathcal{N}(\nu_i, 1, \delta_{\nu_i}) d\nu_i \tag{C.2}$$

where $\mathcal{P}$ stands for a Poissonian distribution of the observed number of events and $ln\mathcal{N}$ for a log-normal distribution of the nuisance parameters ν_i centered at the value 1 with a variance corresponding to a relative error in the background estimation $\delta_{\nu_i}^2 = \delta_{b_i}^2/b_i^2$. The analogous definition is taken for the background-only probability distribution $P(n_i|b_i)$.

The confidence level of the signal+background (backround only) hypothesis is defined as

$$CL_{sb(b)} = \int_{q^{obs}}^{\infty} P_{sb(b)}(q) dq \tag{C.3}$$

where $P_{sb(b)}(q)$ is a probability density of q which corresponds to n_i distributed according to the signal+background (background only) hypothesis and q^{obs} corresponds to the observed number of events n_i^{obs}. Finally the exclusion confidence level for the signal s_i is:

$$CL_{excl} = 1 - \frac{CL_{sb}}{CL_b} \tag{C.4}$$

Obtained in this way confidence intervals coincide with those given in the ref. [50] with a relative deviation of excluded pair-production cross section less than 5%. The difference can be caused by our simplified treatment of the nuisance parameters, i.e. neglecting the signal uncertainties and assuming that the backgrounds of di- and trileptons are completely uncorrelated.

Using the given above definition we find a region in a plane (s_2, s_3) excluded with 95%CL (figure 12).
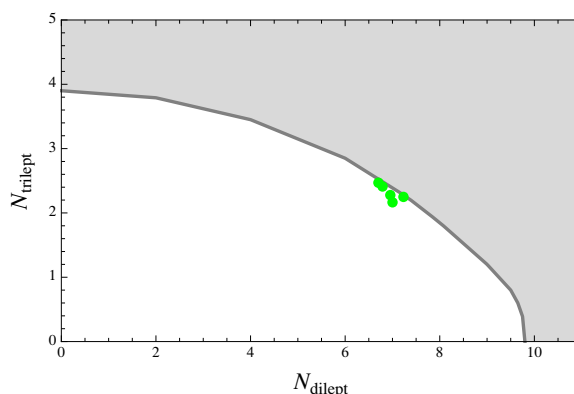
Figure 12. Excluded with 95%CL values of the signal in same-sign dileptons and trileptons channels (gray area) and the maximal allowed values of the di- and trileptons yields according to ref. [50] (green points).

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